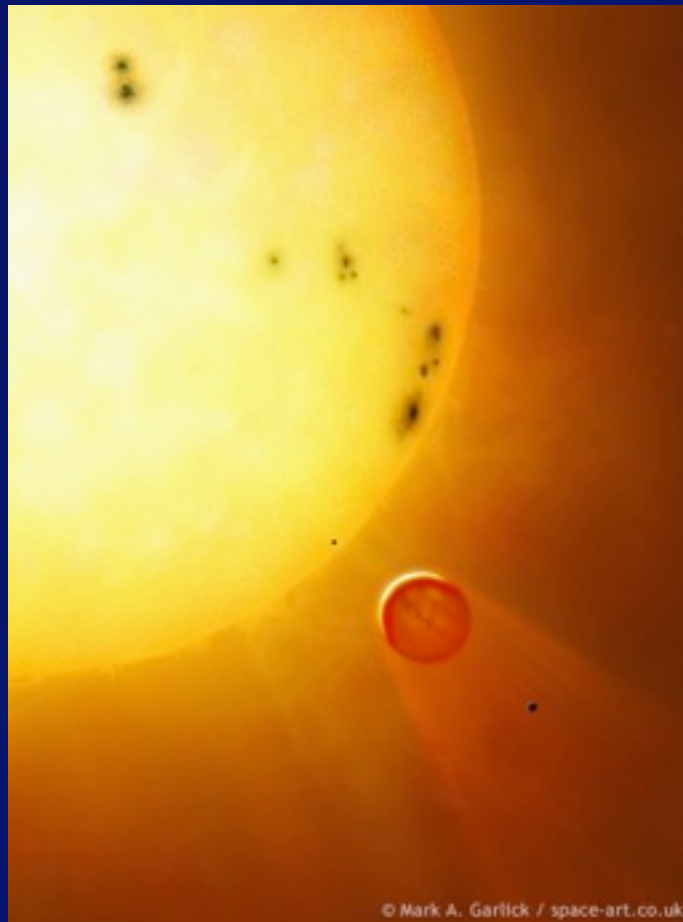



Hydrodynamic Escape from Highly Irradiated Atmospheres



Ruth Murray-Clay
Harvard-Smithsonian Center for Astrophysics

~1% of stars host hot Jupiters

hot Jupiter
~0.05 AU ~ 10 R_*



Sun: $L_{UV} \sim 10^{-6} L_{bol}$
 $\times 10^3$ during T Tauri phase

Mercury
0.39 AU

Earth
1 AU

planets occupy a large
phase space

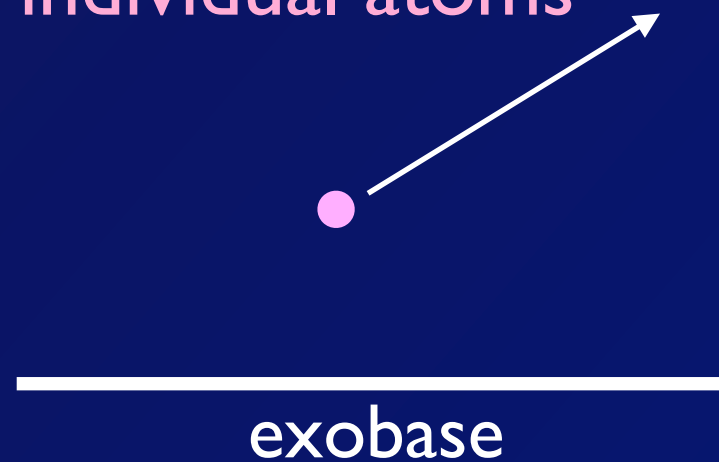
$M_p, R_p, a, L_*, L_{UV,*}, e, \dot{M}_w, B_p$
initial atmosphere

Two classes of escape mechanisms:

Each can be thermal or non-thermal

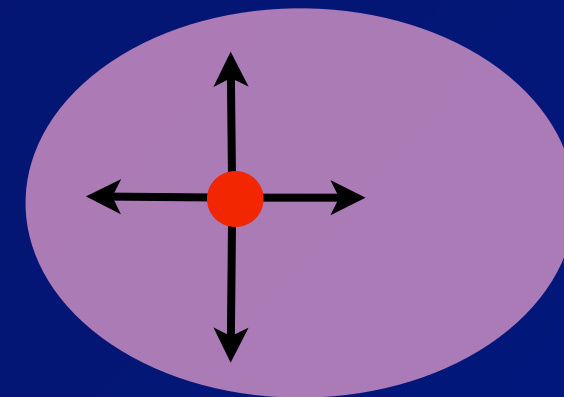
“kinetic”

loss to space of individual atoms



“hydrodynamic”

bulk outflow of a collisional fluid

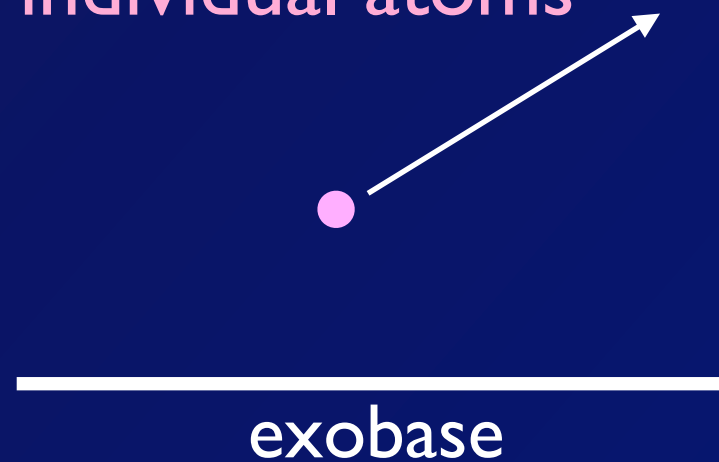


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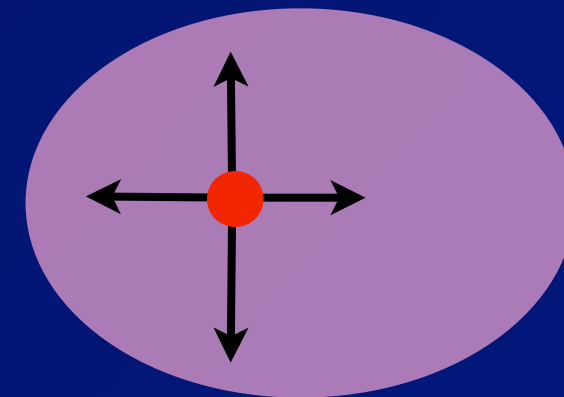
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loss to space of individual atoms



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limits of thermal escape

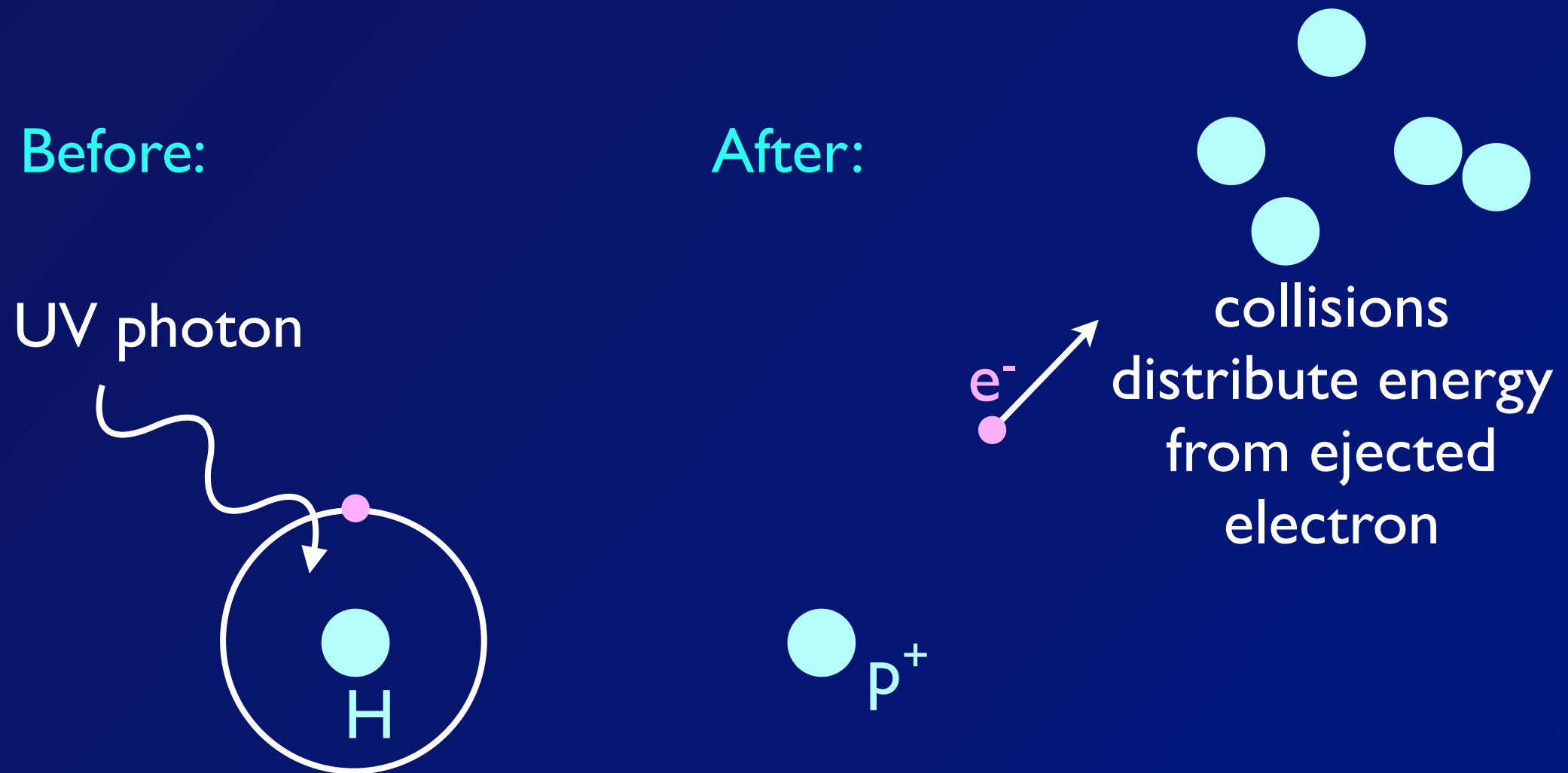
Jeans escape

non-thermal processes, often mediated by B-fields

hydrodynamic escape

Roche lobe overflow
ram pressure stripping

UV photons heat the upper atmosphere by photoionization



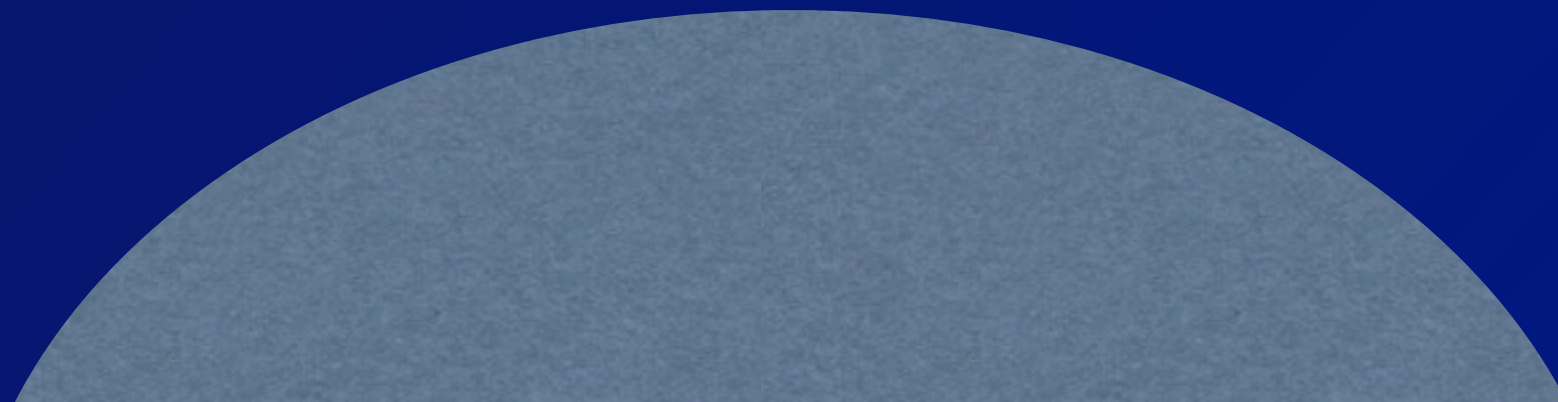
hot Jupiters cannot be evaporated, in spite of early results using “energy-limited escape” models meant for young Earth and Venus

What generates a Parker wind?

fluid,
isothermal

pressure @ $\infty > 0$:
bad!

hydrostatic



What generates a Parker wind?

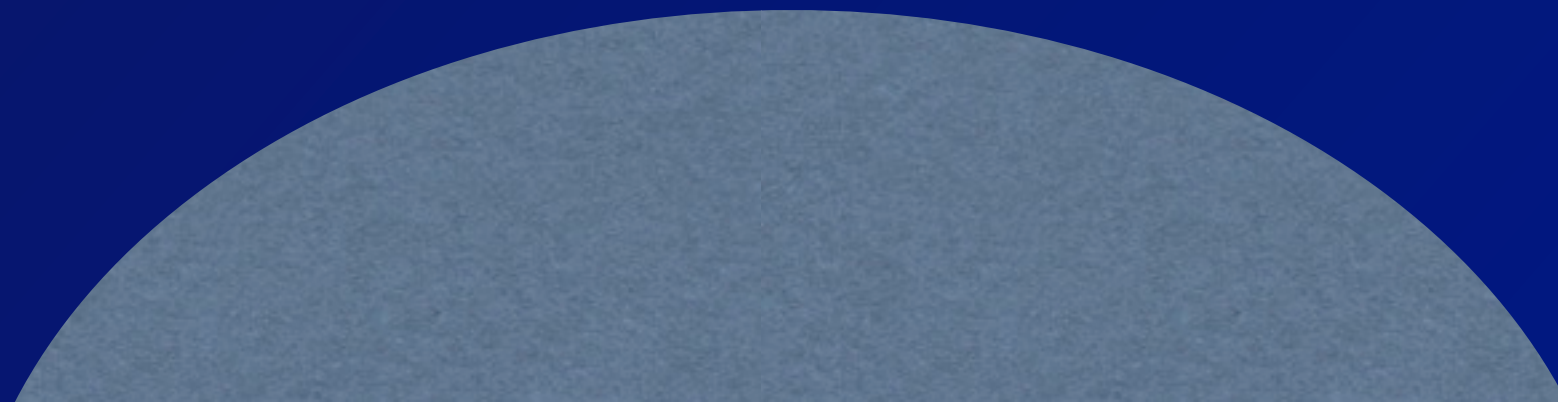
fluid,
isothermal

energy for PdV work in
outward flow comes
from this assumption

pressure @ $\infty > 0$:
bad!

accelerates the gas
outward

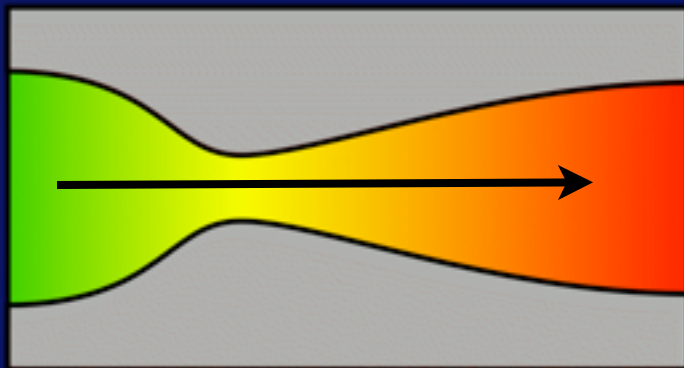
v



Parker winds flow through a critical point

sonic point: $c_s \sim v_{esc}$ **X**

De Laval Nozzle



Von Braun with the Saturn V rocket

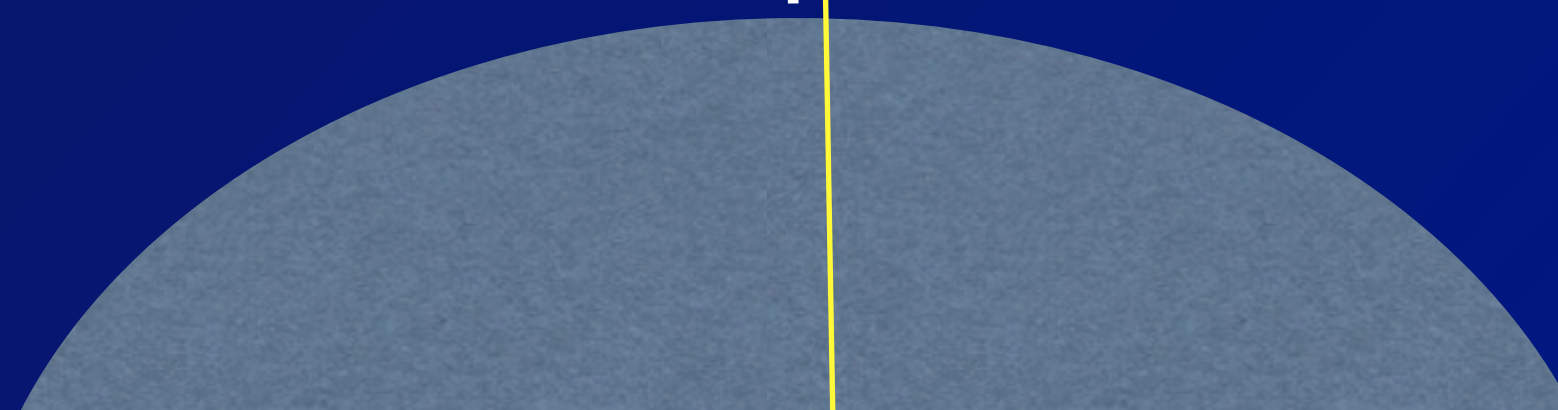
$T \downarrow$:

$$r_s = GM_p / (2c_s^2) \quad \uparrow$$

$$\dot{M} = 4\pi r^2 \rho v \quad \downarrow$$

exponential dropoff

r_s



Drop isothermal assumption

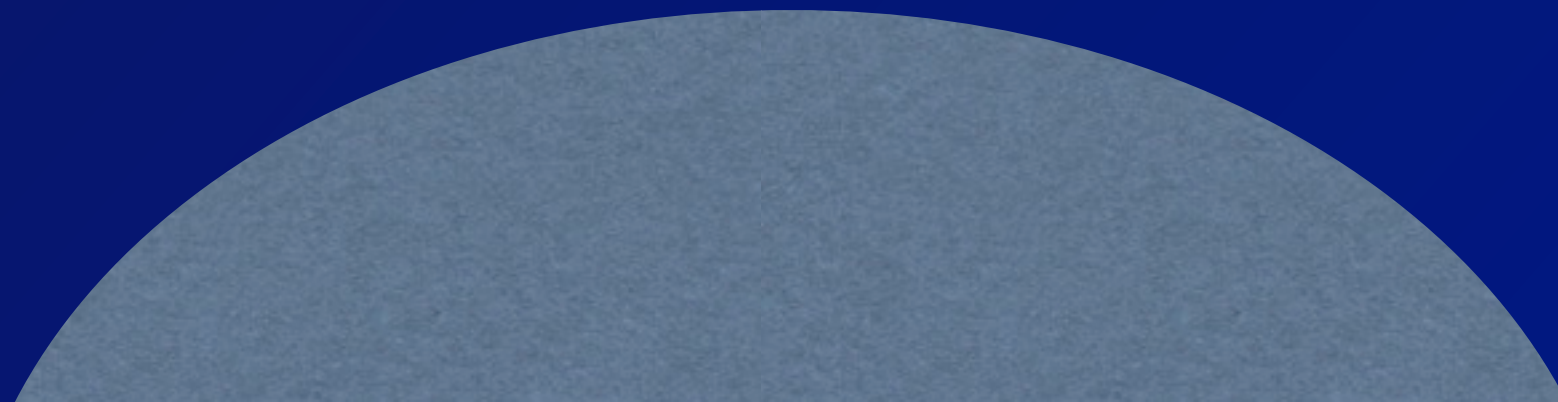
heating from photoionization
sets lower boundary condition

deposited primarily 1
at $\tau \sim 1$: $n_0 \sim \frac{1}{\sigma H}$

still assume fluid (collisional)

only photoionization heating
and pdV work

$P \sim$ nanobars,
altitude set by lower atmosphere



Drop isothermal assumption

heating from photoionization
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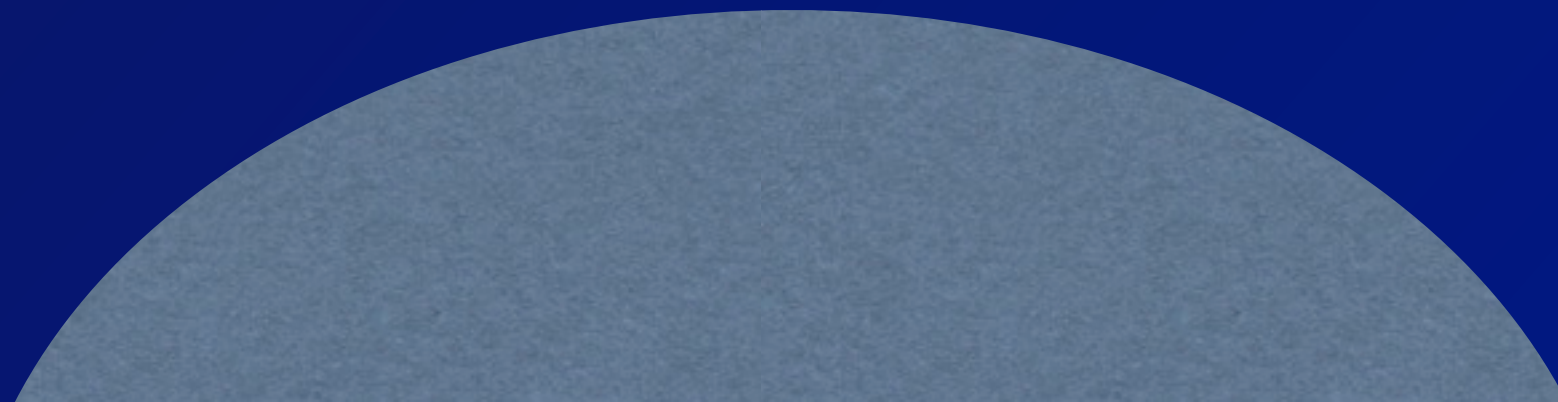
For high UV flux:

$$\frac{F_{UV}}{h\nu_0} \sigma_{\nu_0} n_0 \sim n_+^2 \alpha_{rec}$$

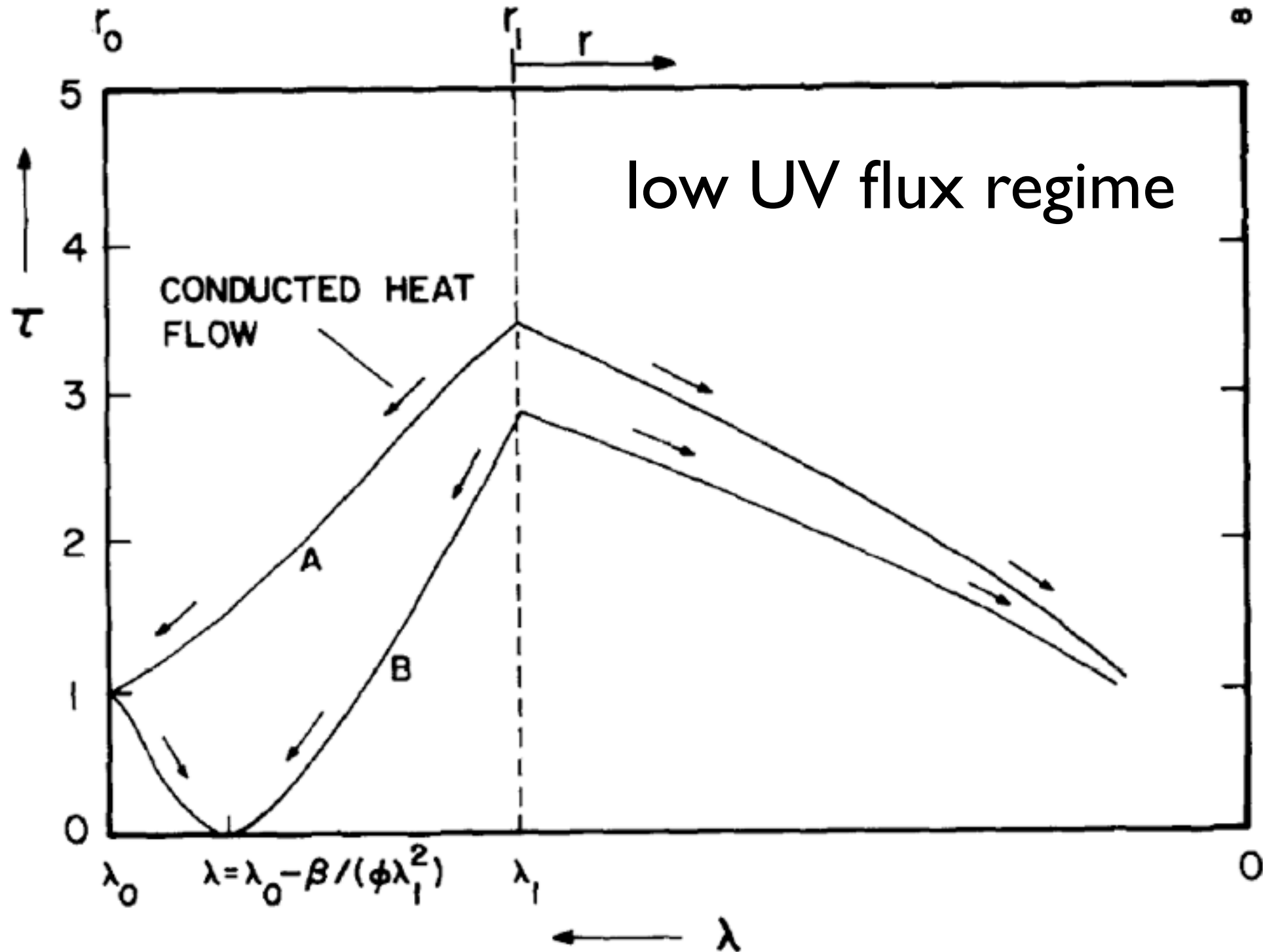
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altitude set by lower atmosphere



Conduction

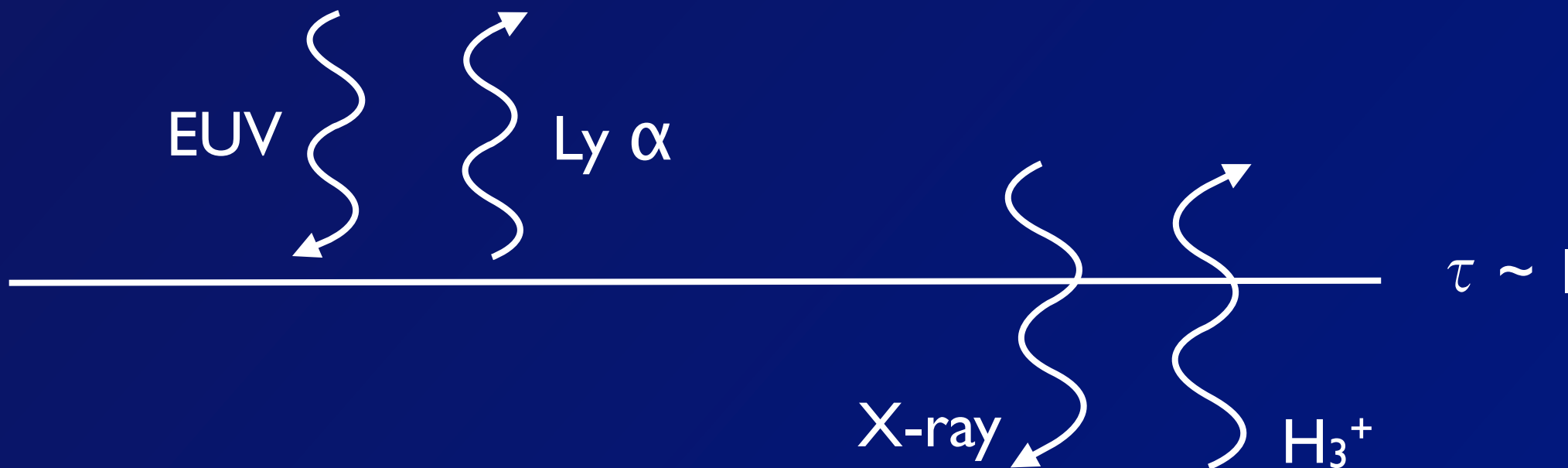


r →

Radiative cooling

$T \sim 10^4 \text{ K}$

EUV Ly α



$T \sim 10^3 \text{ K}$

X-ray H_3^+

$\tau \sim 1$

can kill flow altogether if too high

I haven't cared about the exobase!

If **FUV low** \Rightarrow many scale heights to sonic point;
no longer collisional & model isn't self-consistent

intermediate between
hydrodynamic escape &
Jeans escape:

modified Jeans
escape

fluid outflow
 $v < c_s$

conduction

A diagram illustrating atmospheric escape processes. At the bottom, a grey semi-circle represents the planet's surface. A vertical white arrow points upwards from the surface, labeled 'conduction'. Above this arrow, the text 'fluid outflow' is written, with the inequality $v < c_s$ below it. At the top of the vertical arrow is a small pink dot. From this dot, a white arrow points diagonally upwards and to the right, labeled 'modified Jeans escape'.

Hot Jupiter

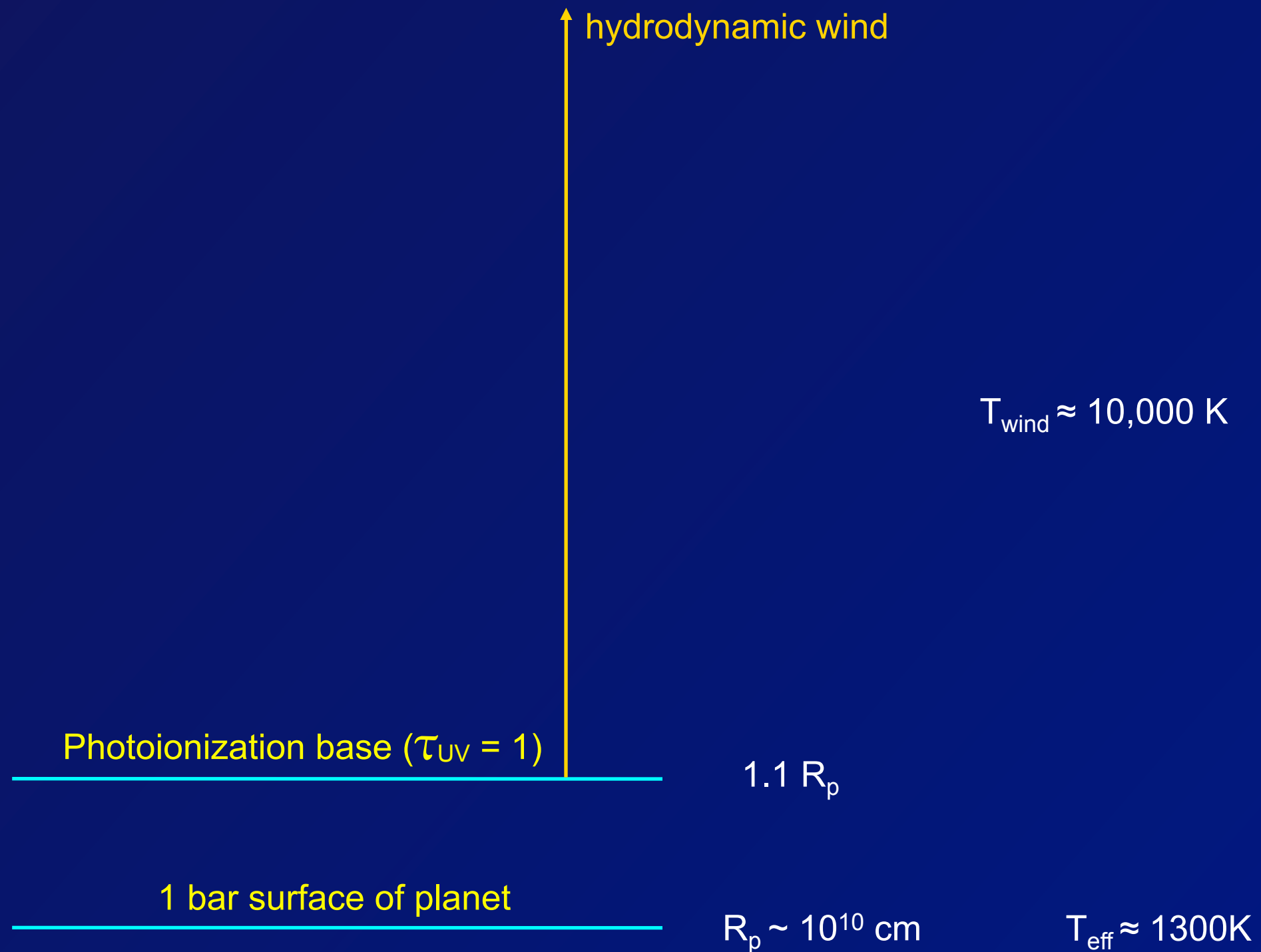
1 bar surface of planet



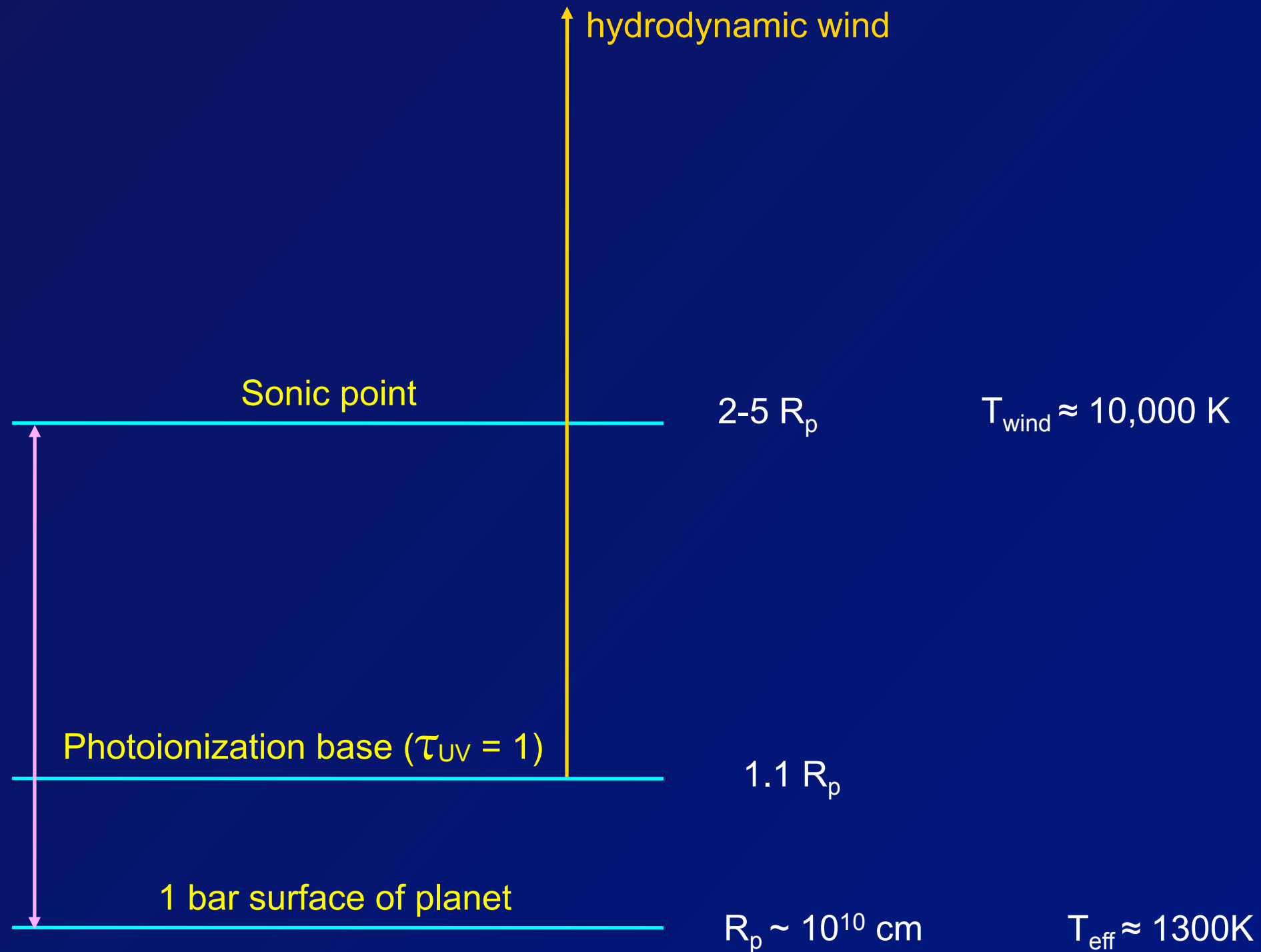
$$R_p \sim 10^{10} \text{ cm}$$

$$T_{\text{eff}} \approx 1300\text{K}$$

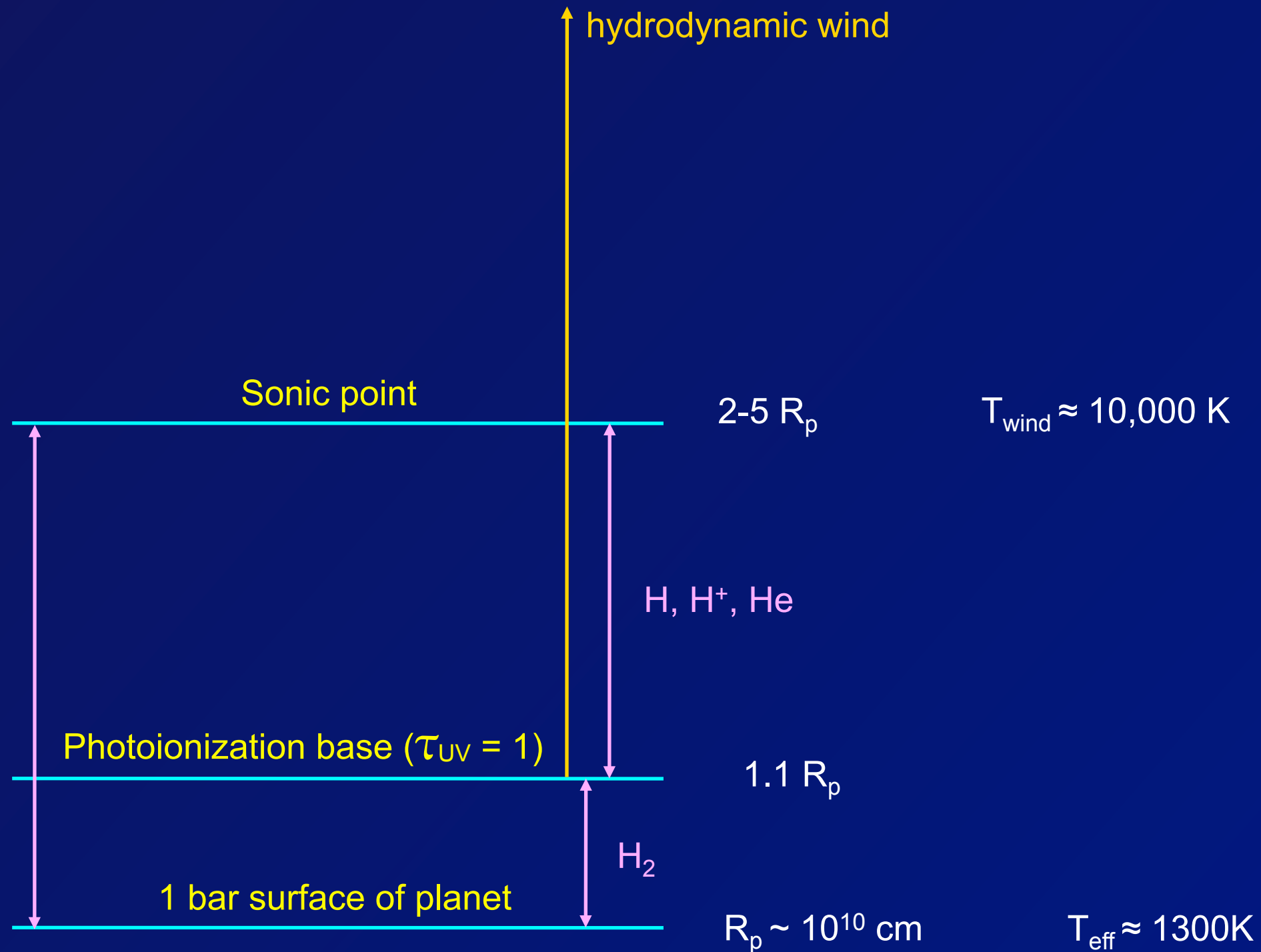
Hot Jupiter



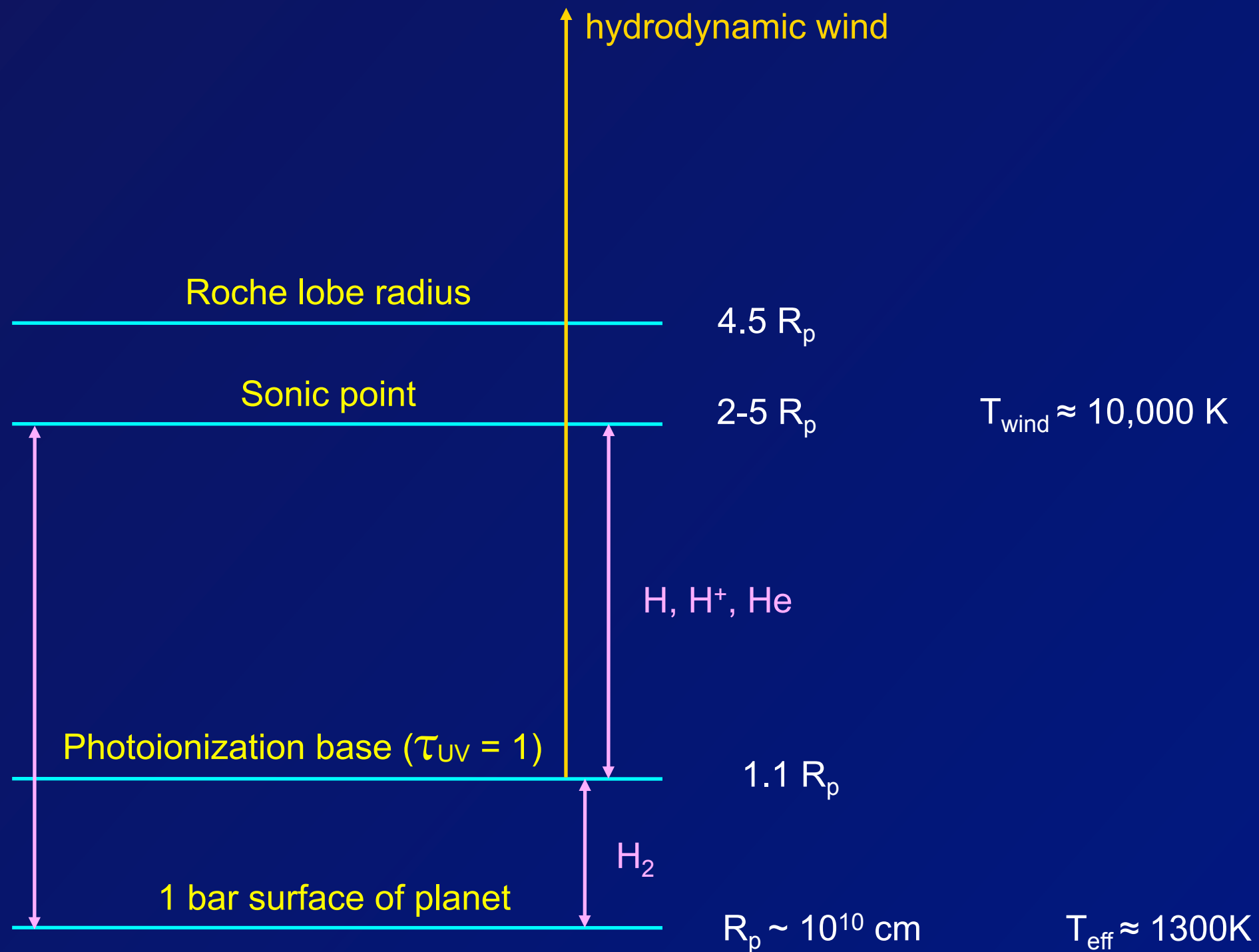
Hot Jupiter



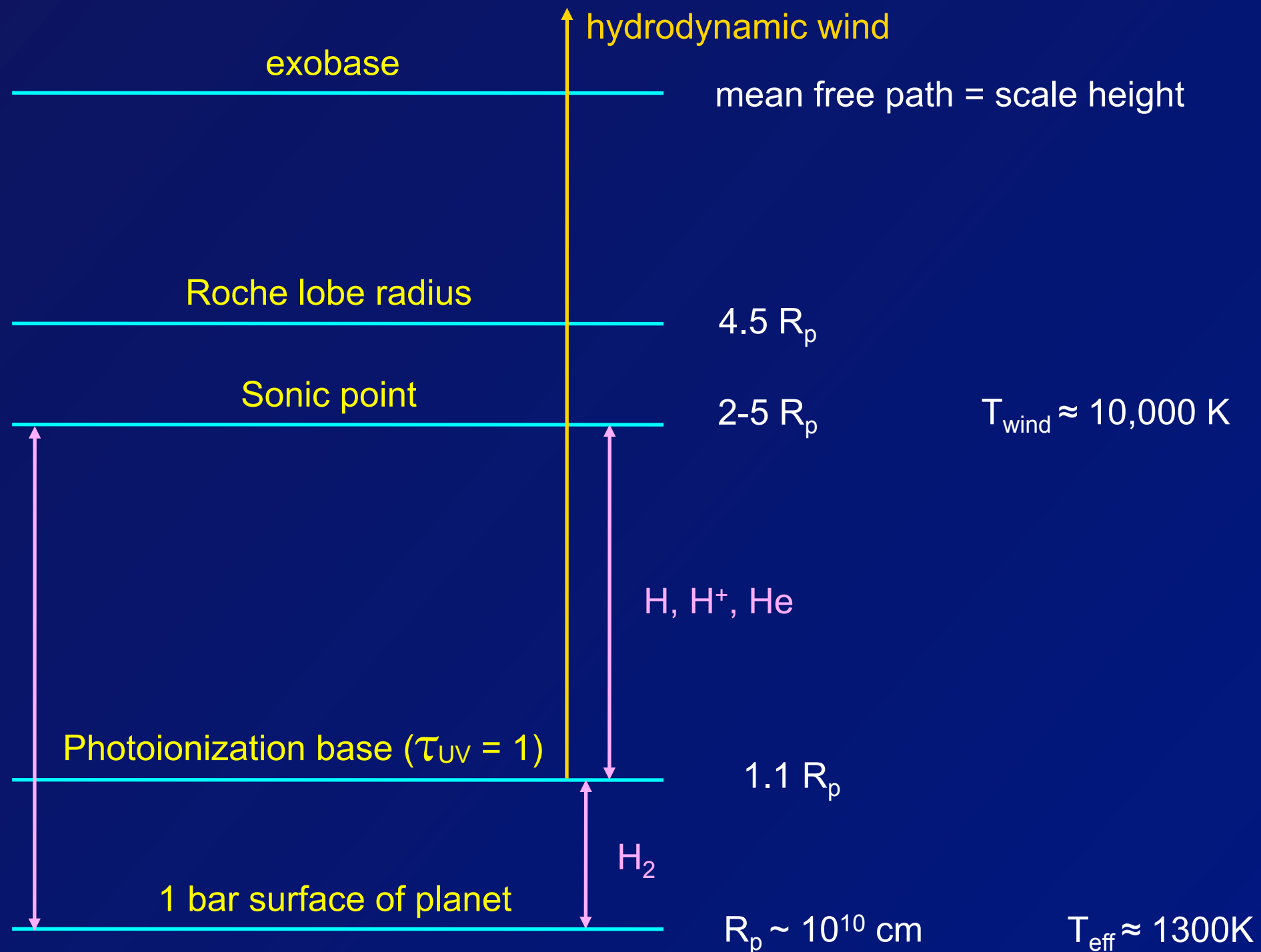
Hot Jupiter



Hot Jupiter



Hot Jupiter



Hydrodynamic Escape Equations

Mass continuity: $\frac{\partial}{\partial r}(r^2 \rho v) = 0$

Momentum: $\rho v \frac{\partial v}{\partial r} = -\frac{\partial P}{\partial r} - \frac{GM_p \rho}{r^2} + \frac{3GM_* \rho r}{a^3}$

Energy: $\rho v \frac{\partial}{\partial r} \left[\frac{kT}{(\gamma - 1)\mu} \right] = \frac{kT v}{\mu} \frac{\partial \rho}{\partial r} + \epsilon F_{\nu_0} e^{-\tau} a_{\nu_0} n_0 + \Lambda$

Ionization equilibrium:

$$n_0 \frac{F_{\nu_0} e^{-\tau}}{h\nu_0} a_{\nu_0} = n_+^2 \alpha_{\text{rec}} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 n_+ v)$$

Solved using a relaxation code

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Photoionization heating
+ Ly α cooling

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Solved using a relaxation code

Consistently solves ionization and energy equations.

Can be used for different regimes.

General boundary conditions

- Critical (sonic) point of transsonic wind (2 conditions)
- ionization fraction at depth is small
- density at depth is large enough that $\tau \gg 1$
- temperature at depth is $< 10^4$ K
- self consistent optical depth to ionization

Solution for the current HD 209458b

Murray-Clay et al. 2009

$$M_p = 0.7 M_J$$

$$R_p = 1.4 R_J$$

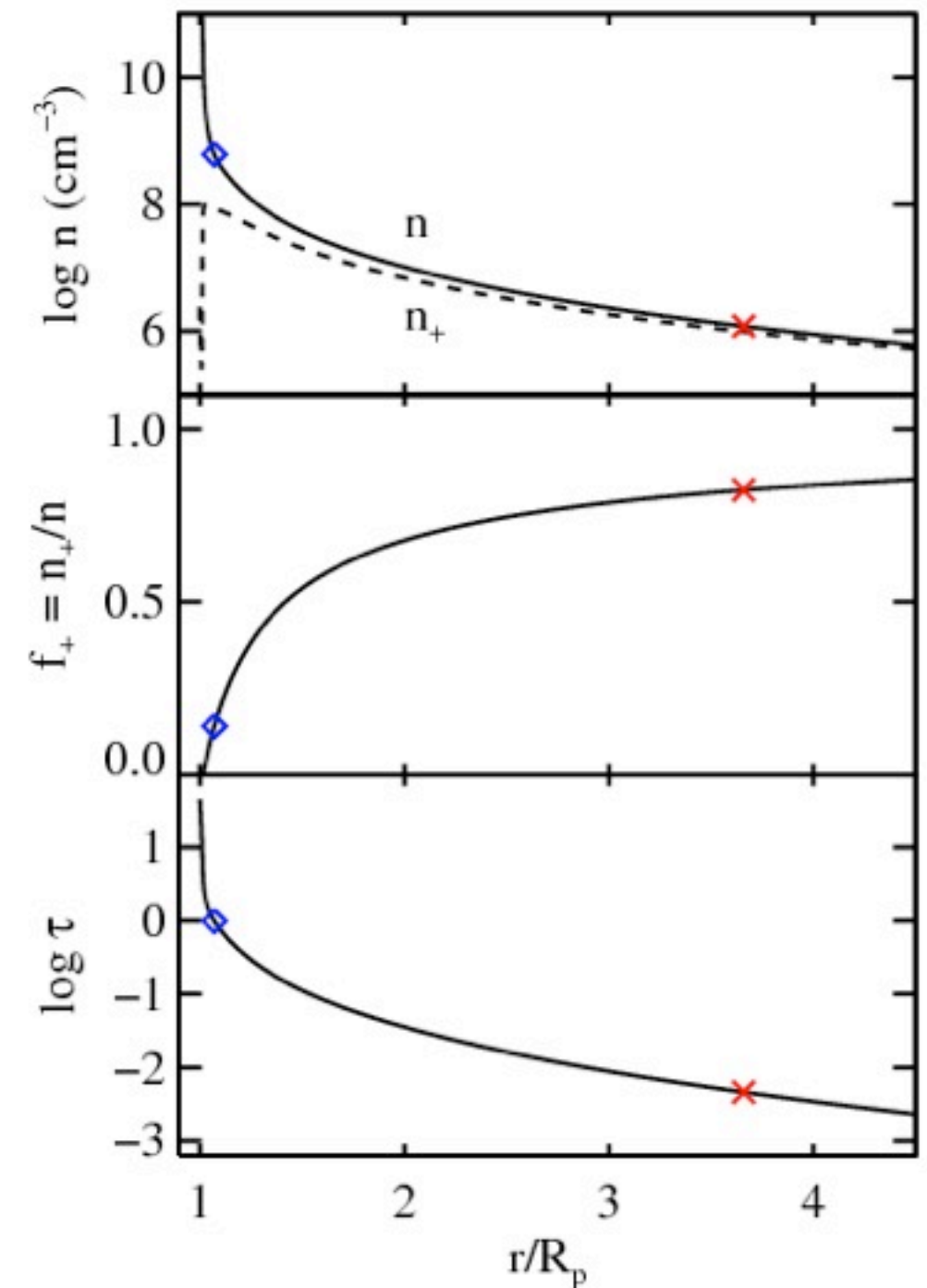
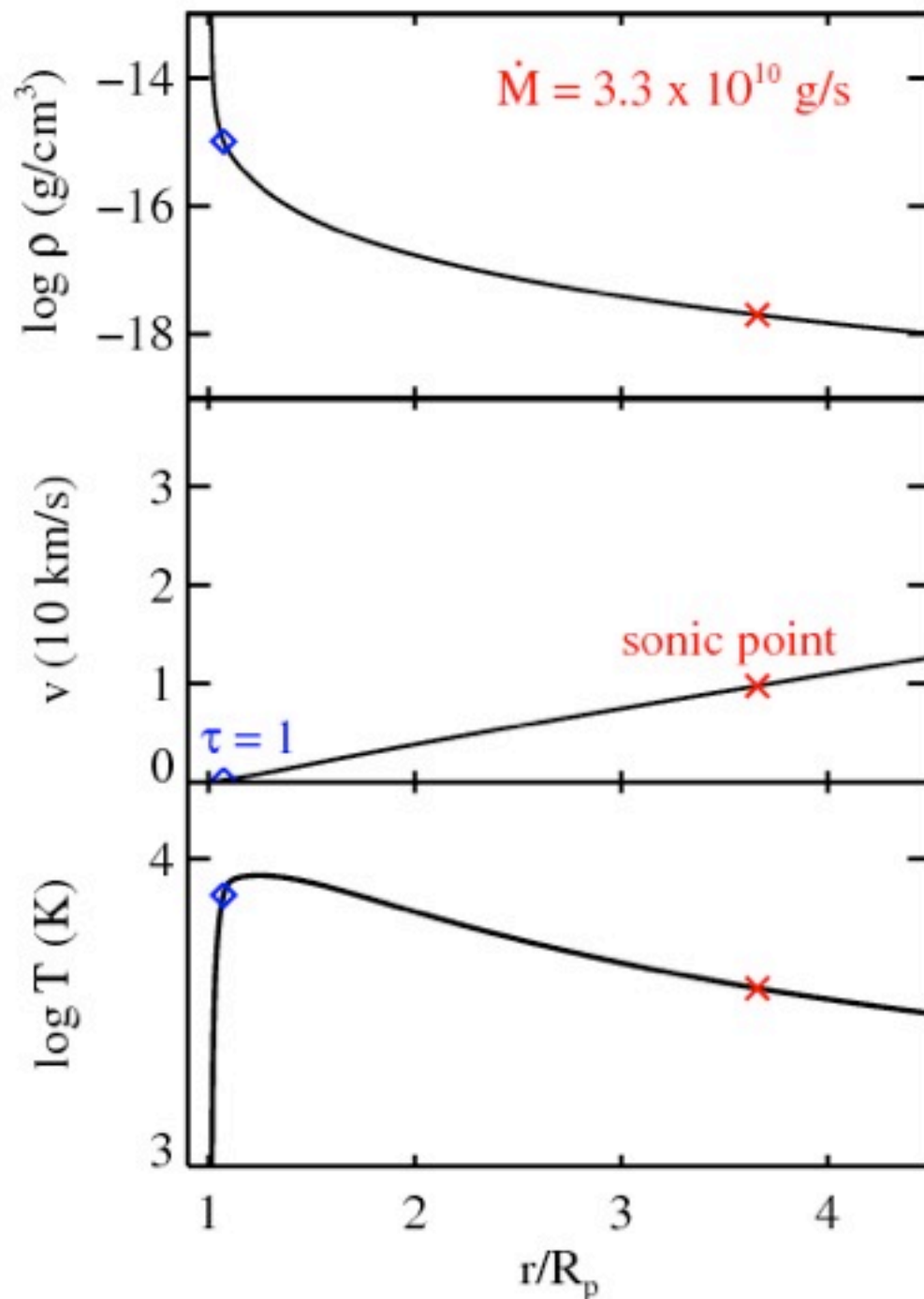
$$h\nu_0 = 20\text{eV}$$

$$\rho_{\text{base}} = 4 \times 10^{-13} \text{ g}$$

$$T_{\text{base}} = 1000 \text{ K}$$

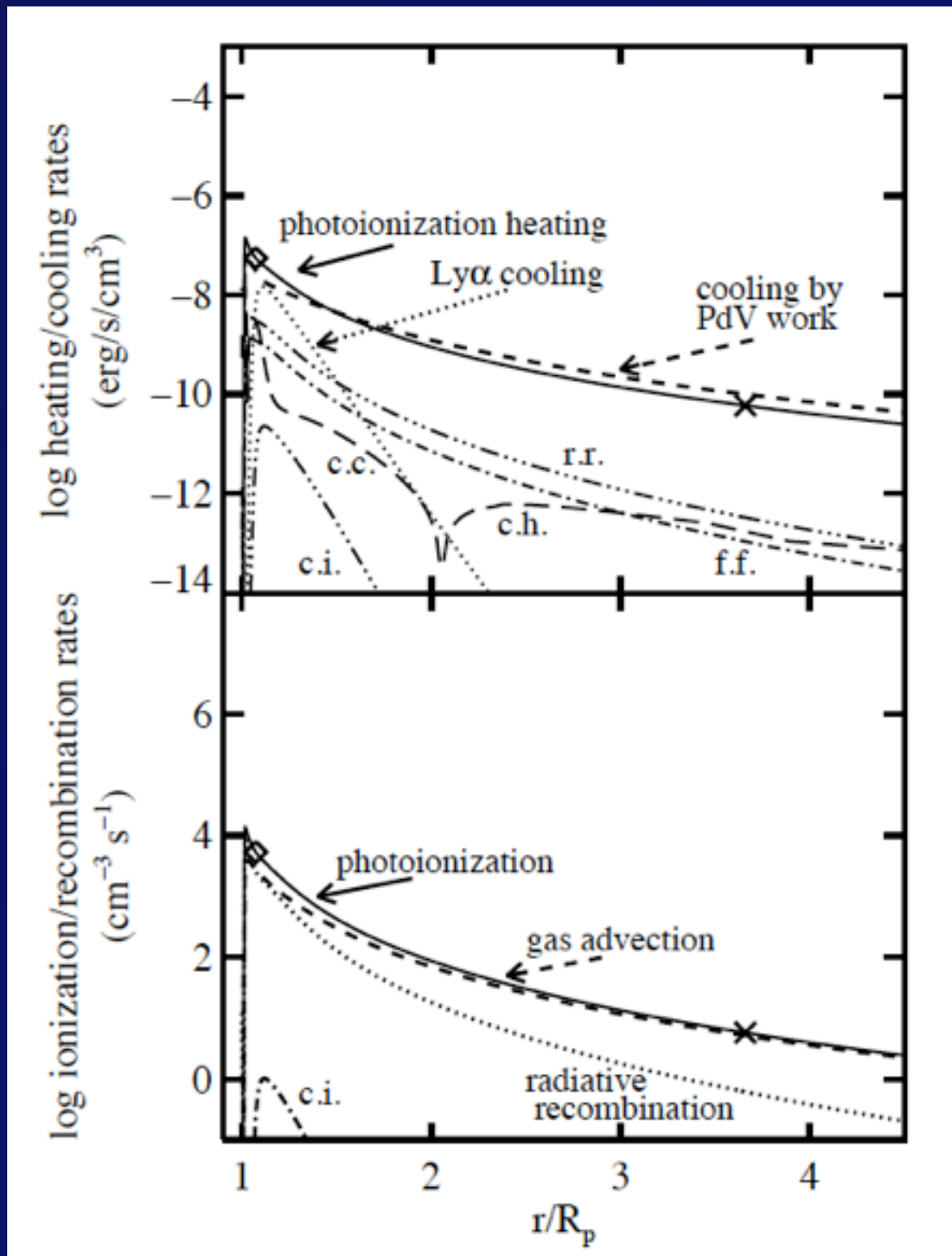
$$f_{\text{base}} = 10^{-5}$$

$$\tau_{\text{sp}} = 0.0046$$

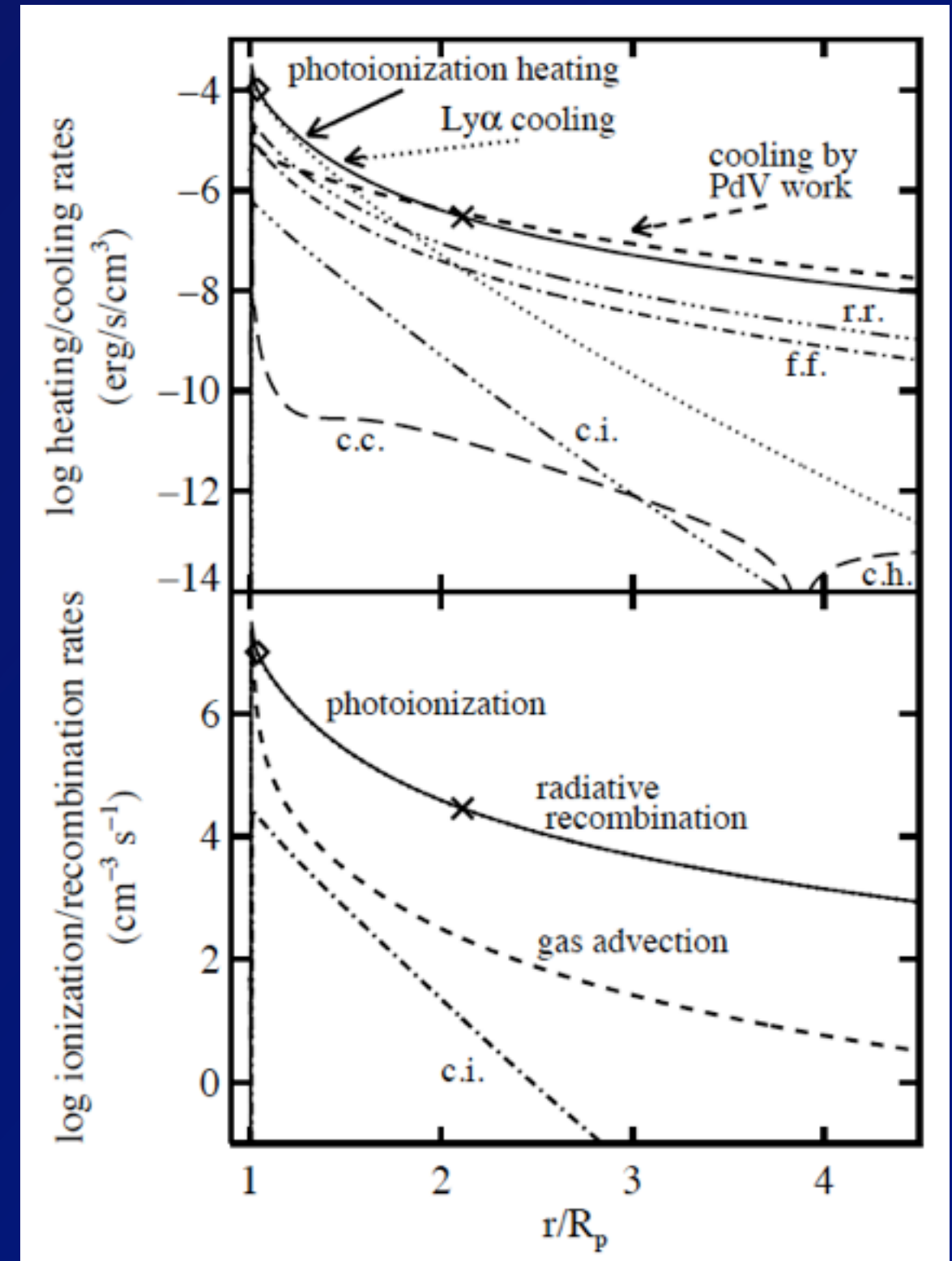


$$F_{\text{UV}} = 450 \text{ erg/cm}^2/\text{s}$$

Energy and ionization balance



Solar FUV



T Tauri FUV

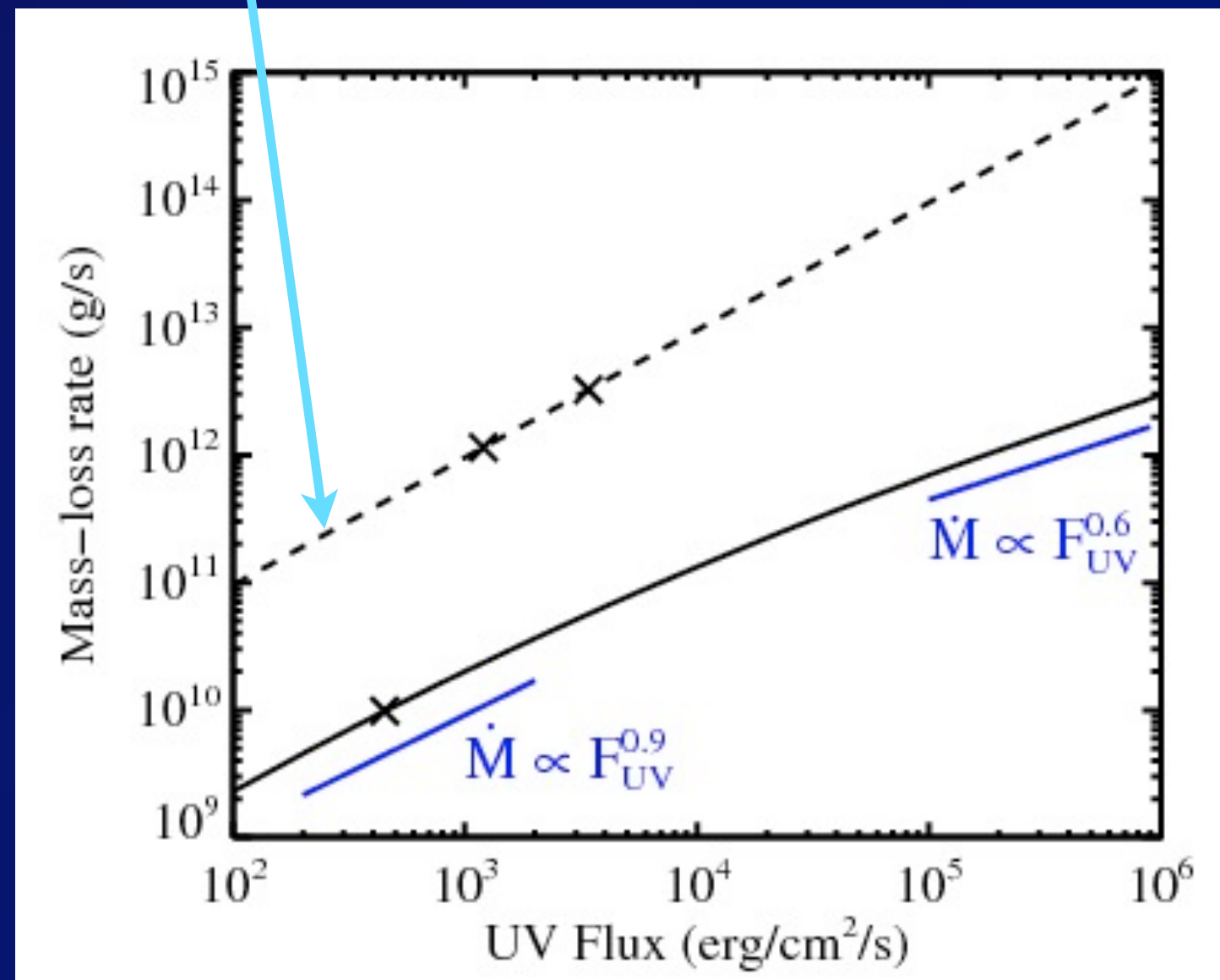
Mass-Loss Rates: Dependence on UV Flux

Murray-Clay et al. 2009

$$\dot{M} = \frac{\pi F_{\text{UV}} (3R_{\text{P}})^3}{GM_{\text{p}}}$$

$$\dot{M} \sim 3 \times 10^{12} \text{ g/s}$$

HD 209458b:
T Tauri
~ 0.1% loss



HD 209458b:
main sequence
~ 1% loss

$$\dot{M} \sim 10^{10} \text{ g/s}$$

Mass-Loss Rates: Dependence on UV Flux

Murray-Clay et al. 2009

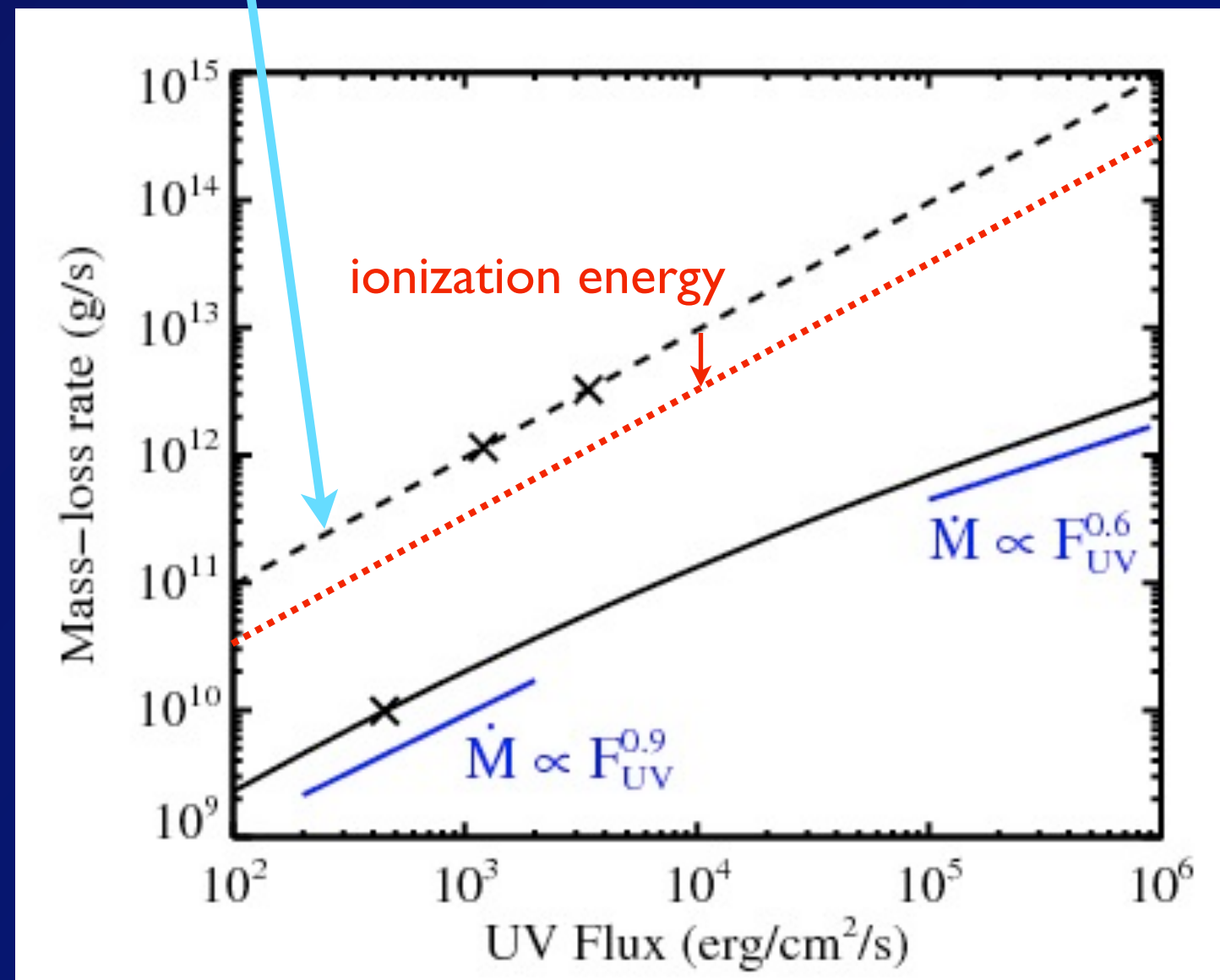
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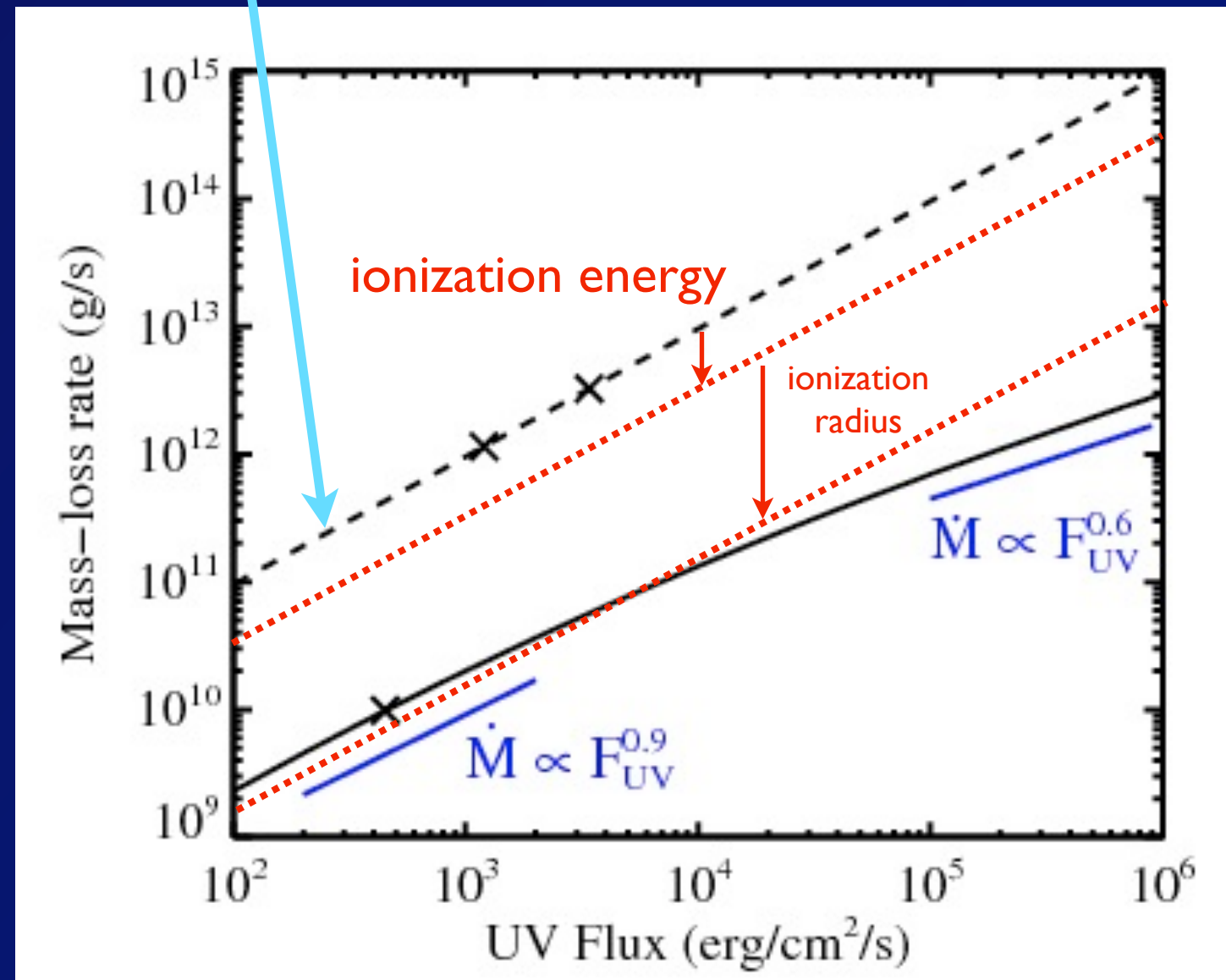
$$\dot{M} = \frac{\epsilon F_{UV} 1R_P}{\pi F_{UV} (3R_P)^3 GM_p}$$

$$\dot{M} \sim 3 \times 10^{12} \text{ g/s}$$

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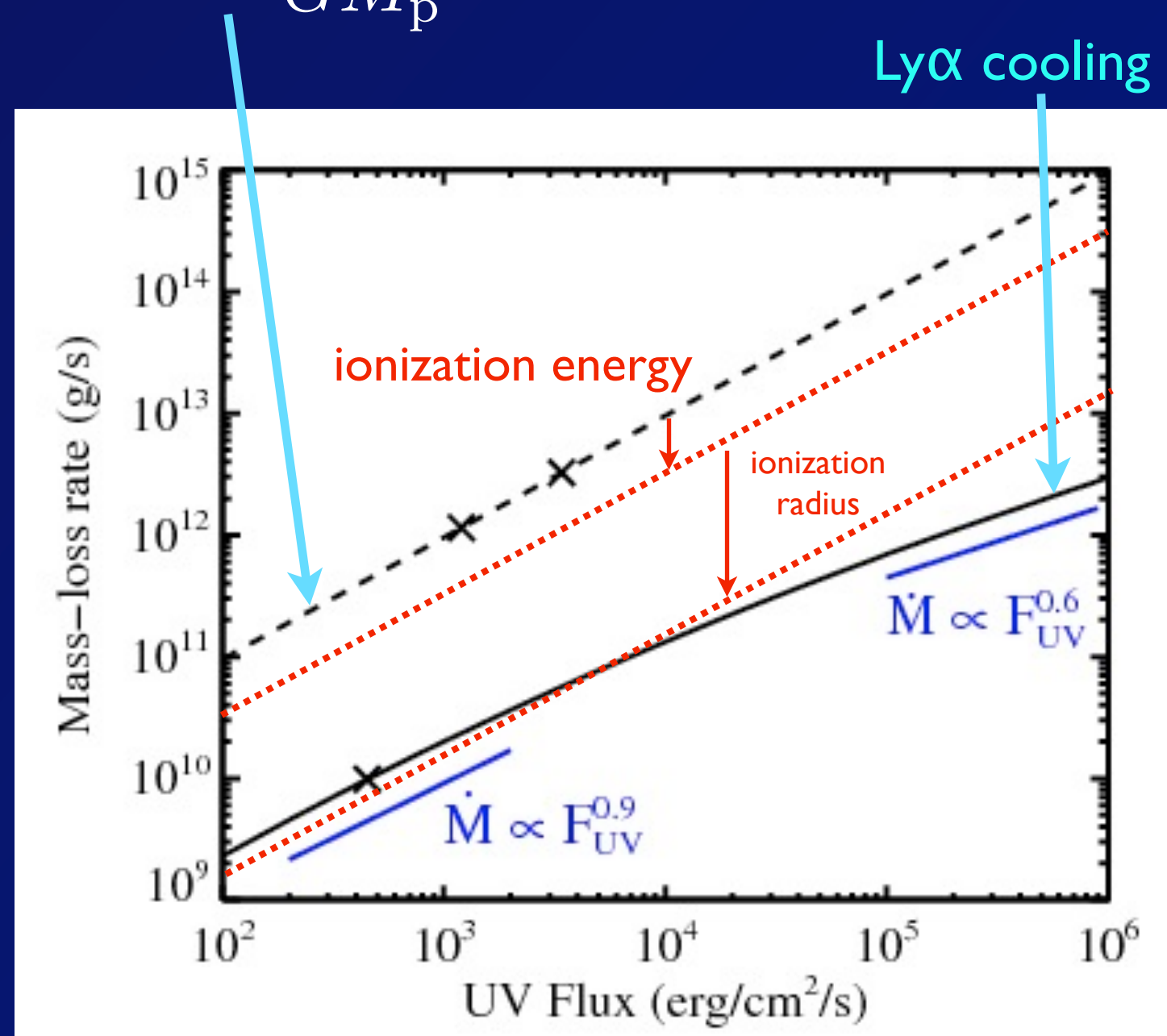
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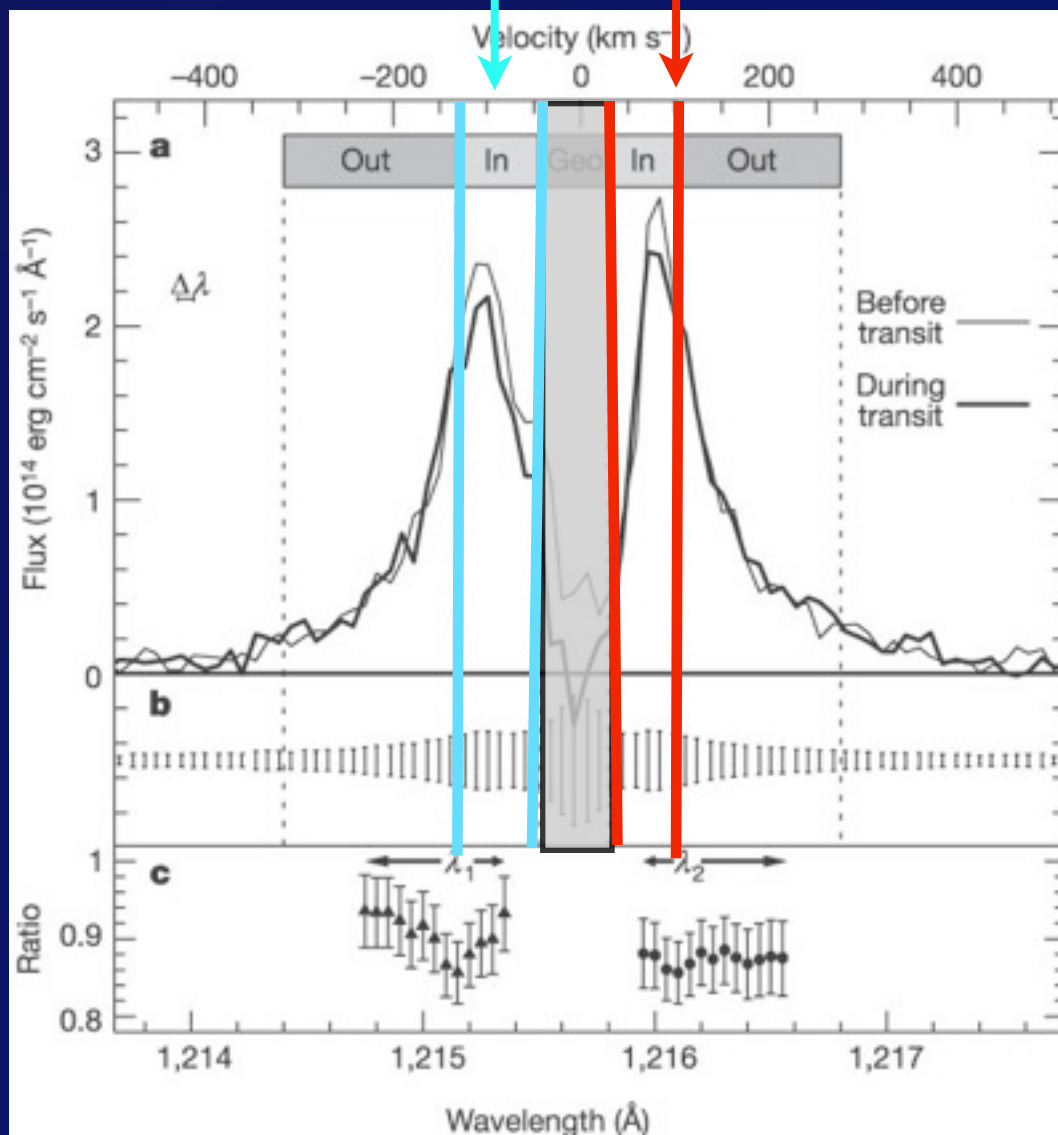
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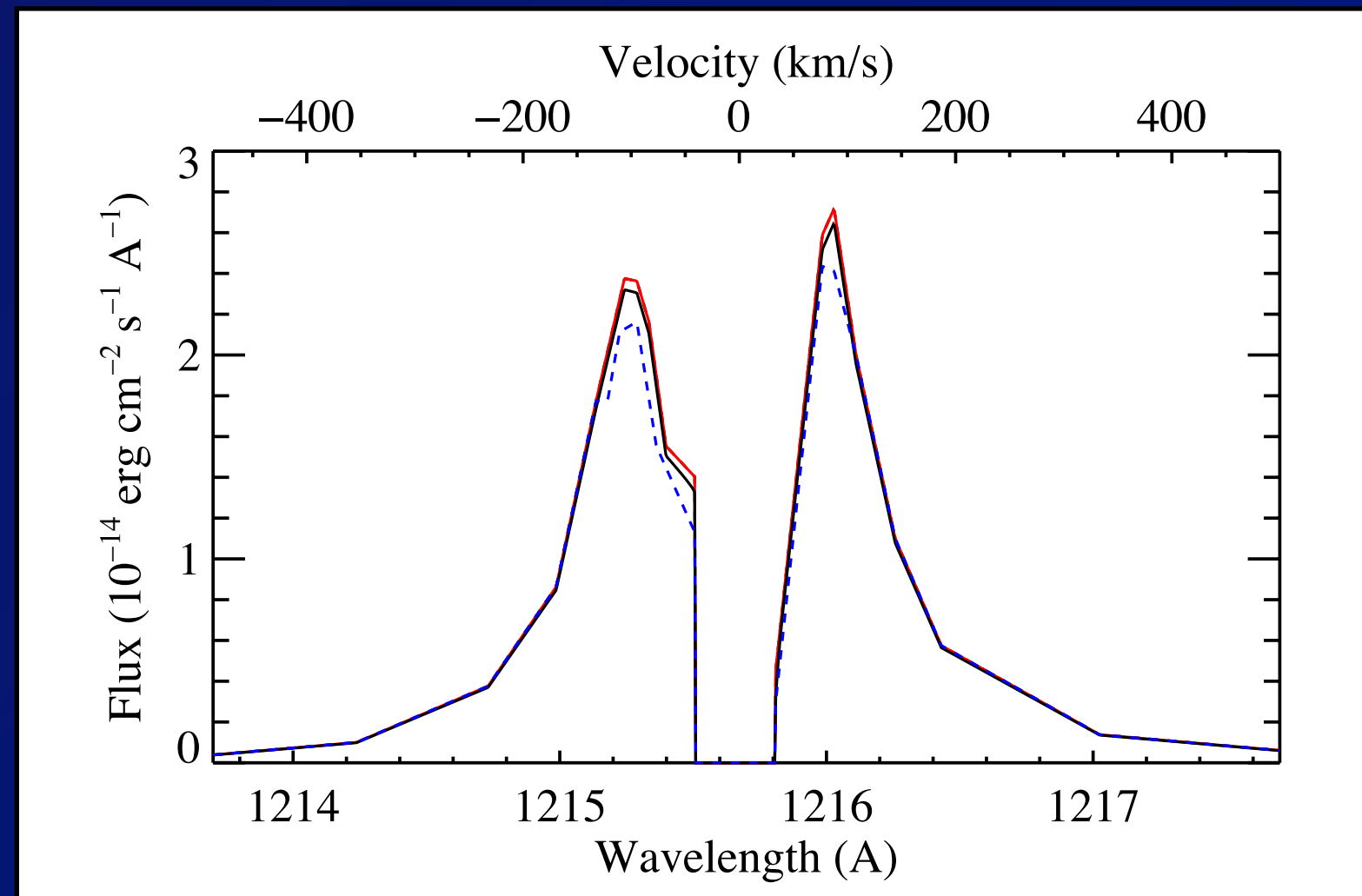


The wind cannot directly generate enough absorption at ± 100 km/s to reproduce measurements of HD 209458b.

-100 km/s 100 km/s

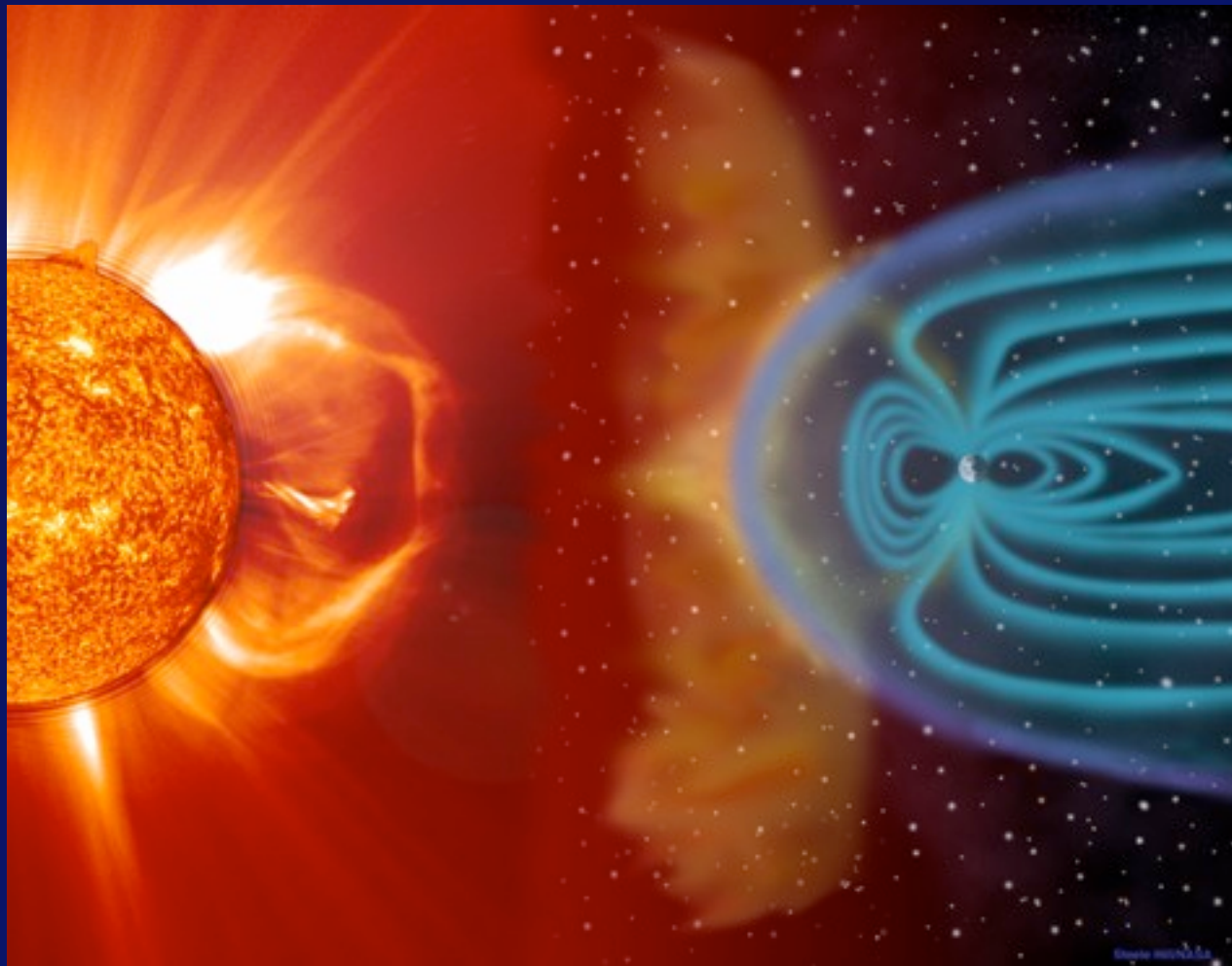


Vidal-Madjar et al. 2003



Murray-Clay, Chiang, & Murray 2009

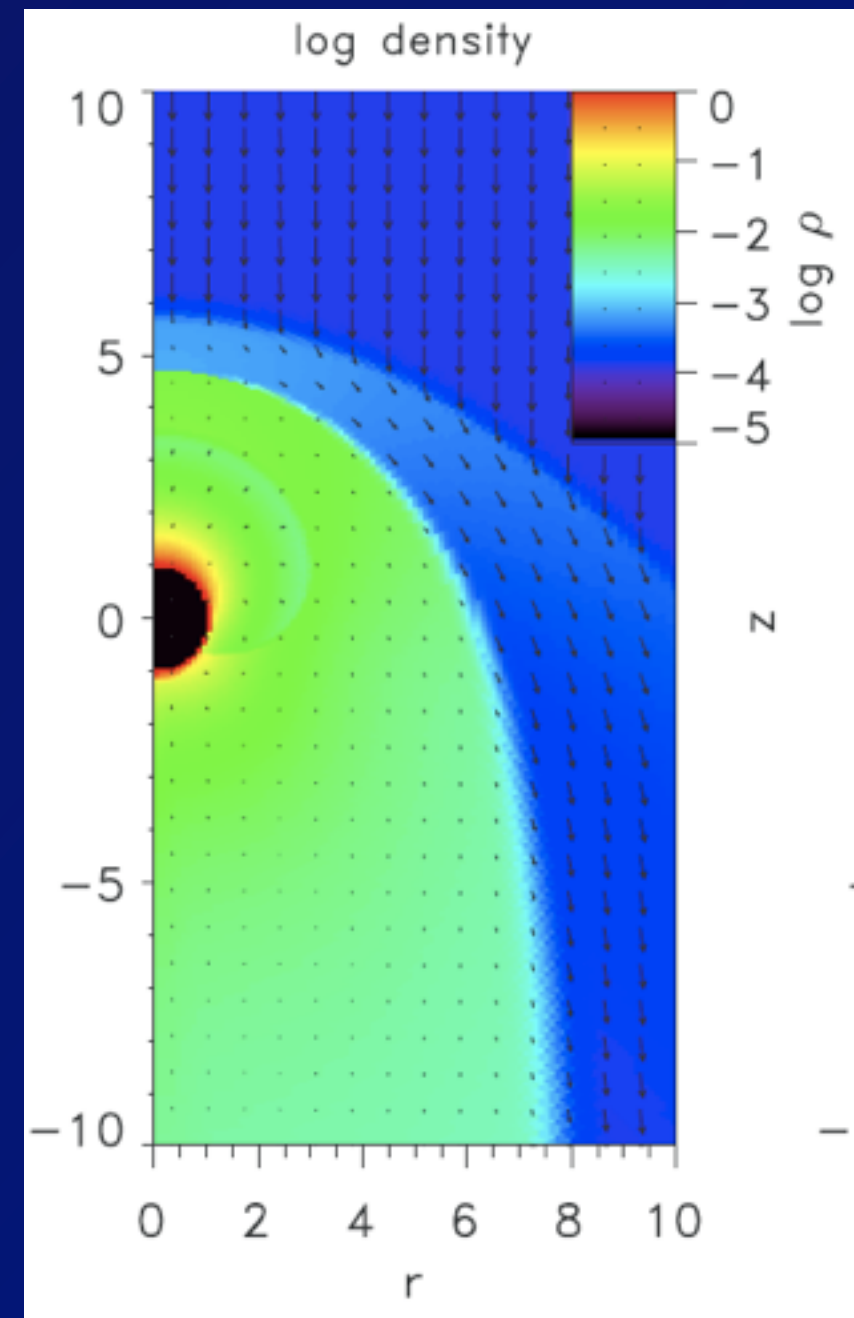
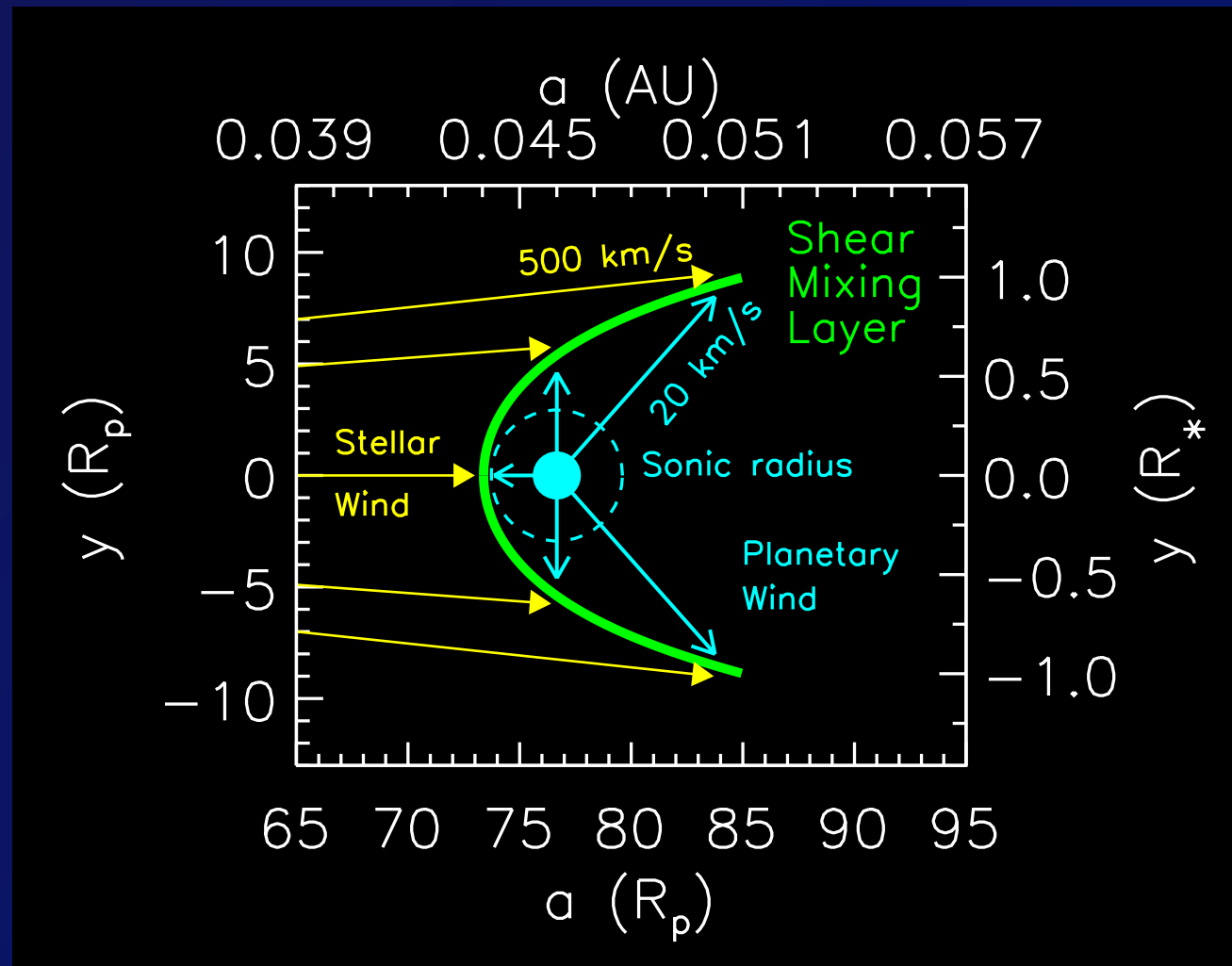
What about the stellar wind and the planetary magnetic field?



NASA



NASA

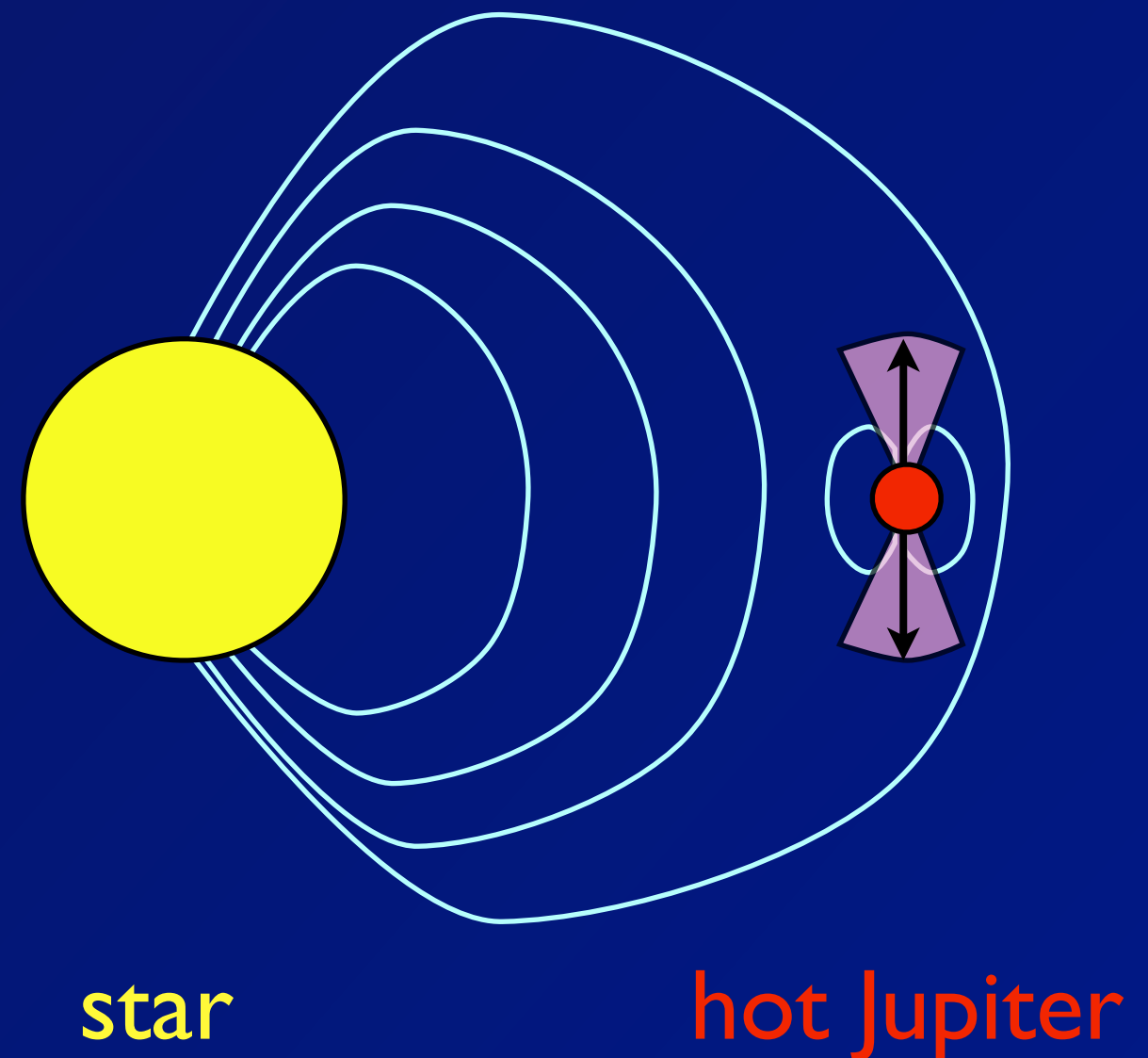
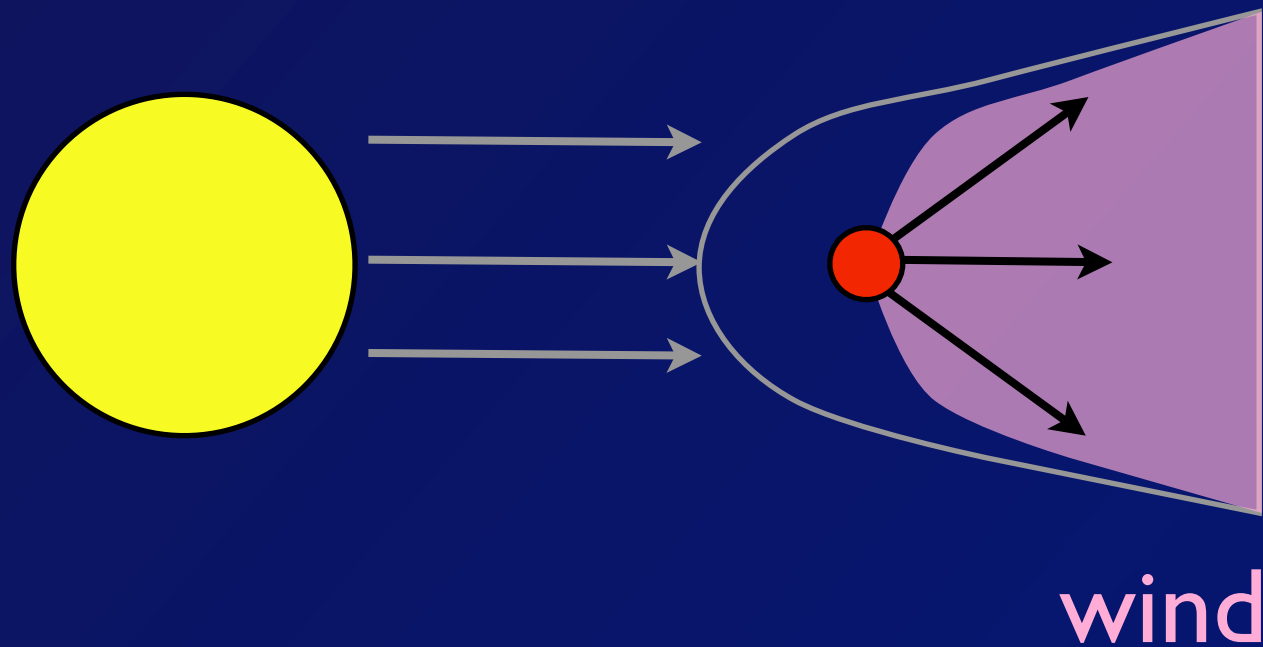


Stone & Proga 2009

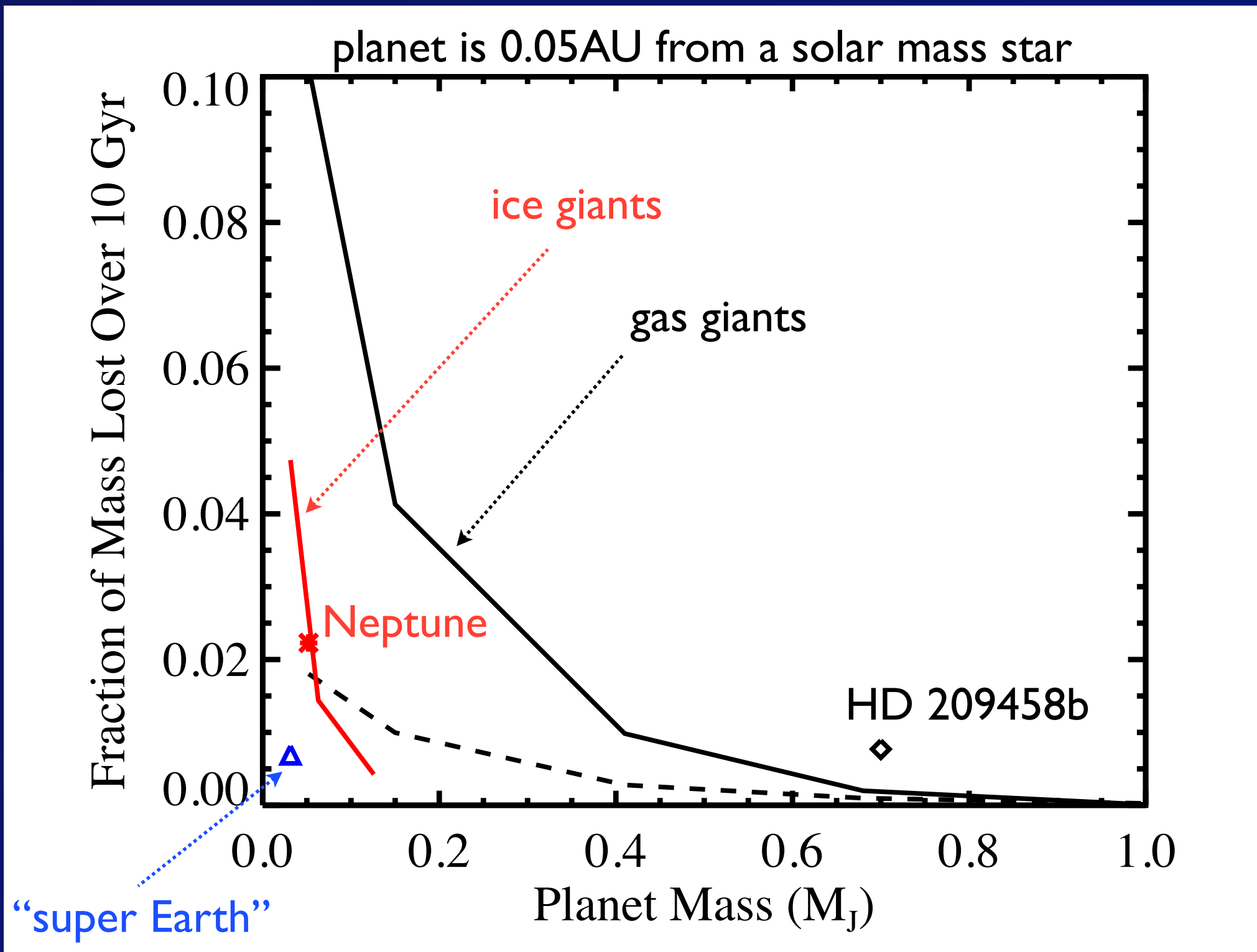
Possibilities to explain the observations:

- charge-exchange in the shock or planetary magnetosphere generates high-velocity neutrals
- 3D effects increase the neutral column

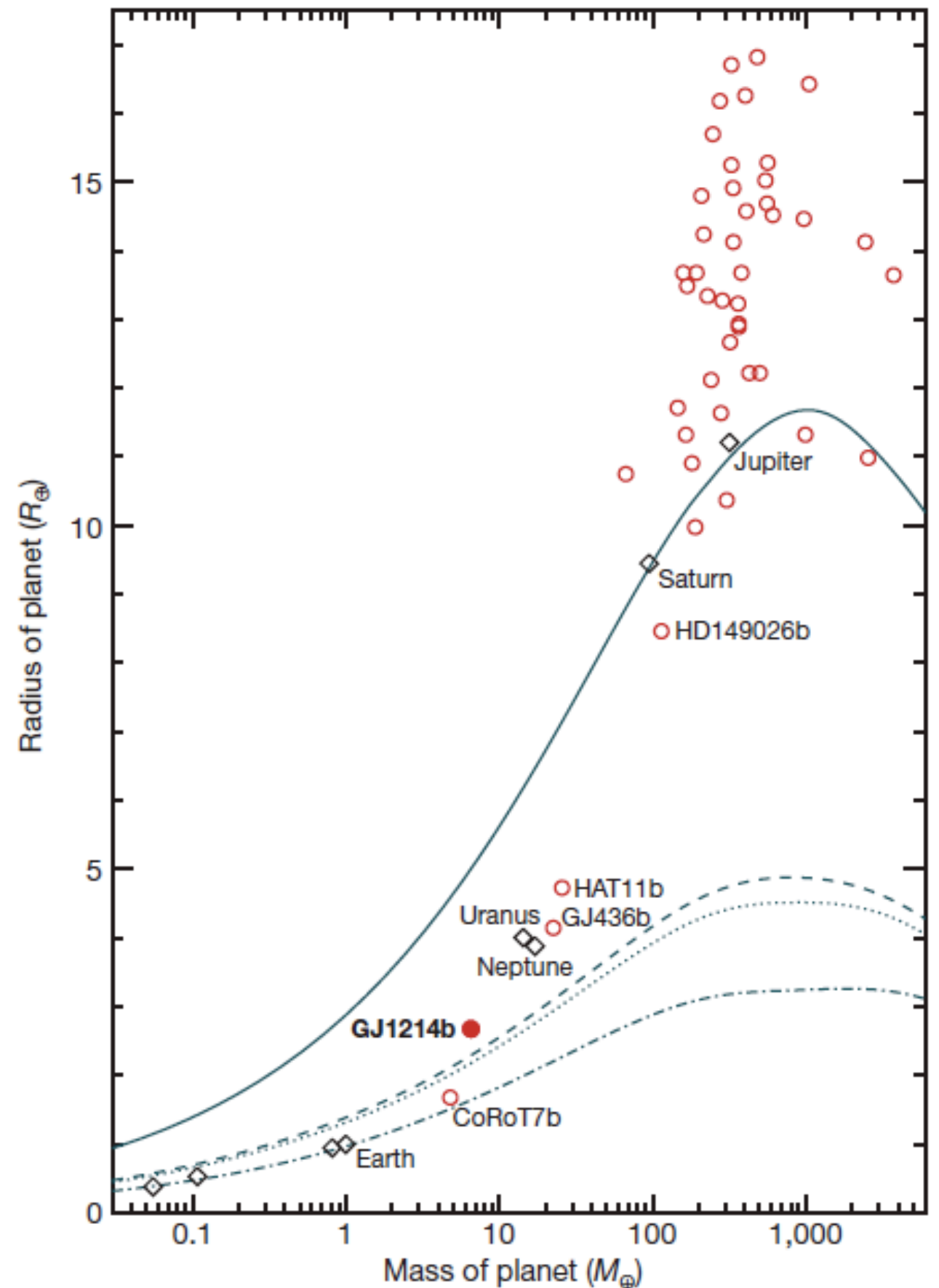
Both the stellar wind ram pressure and magnetic fields can reduce and/or shape mass loss



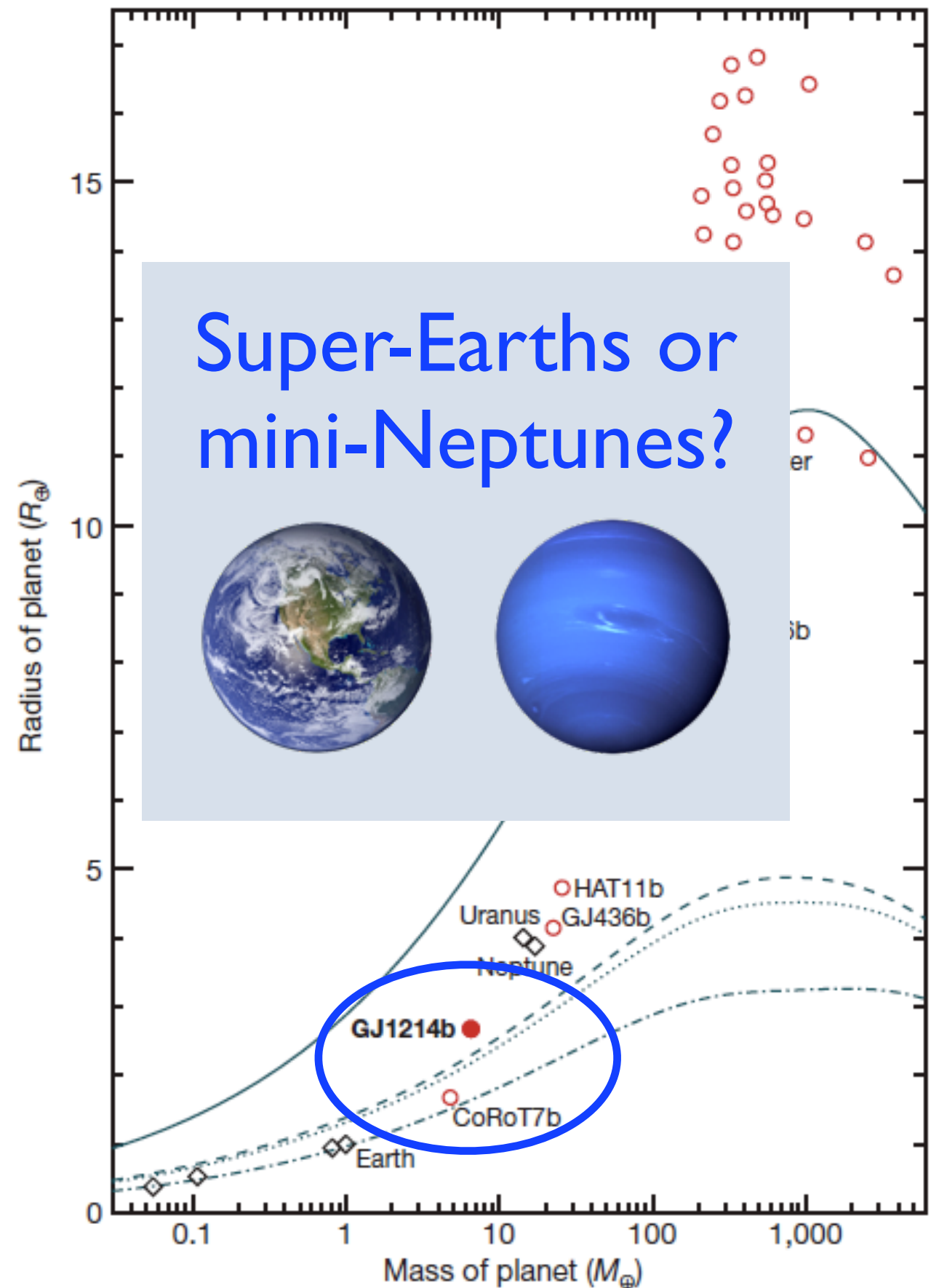
Low mass gas giants and the atmospheres of solid planets can be significantly depleted



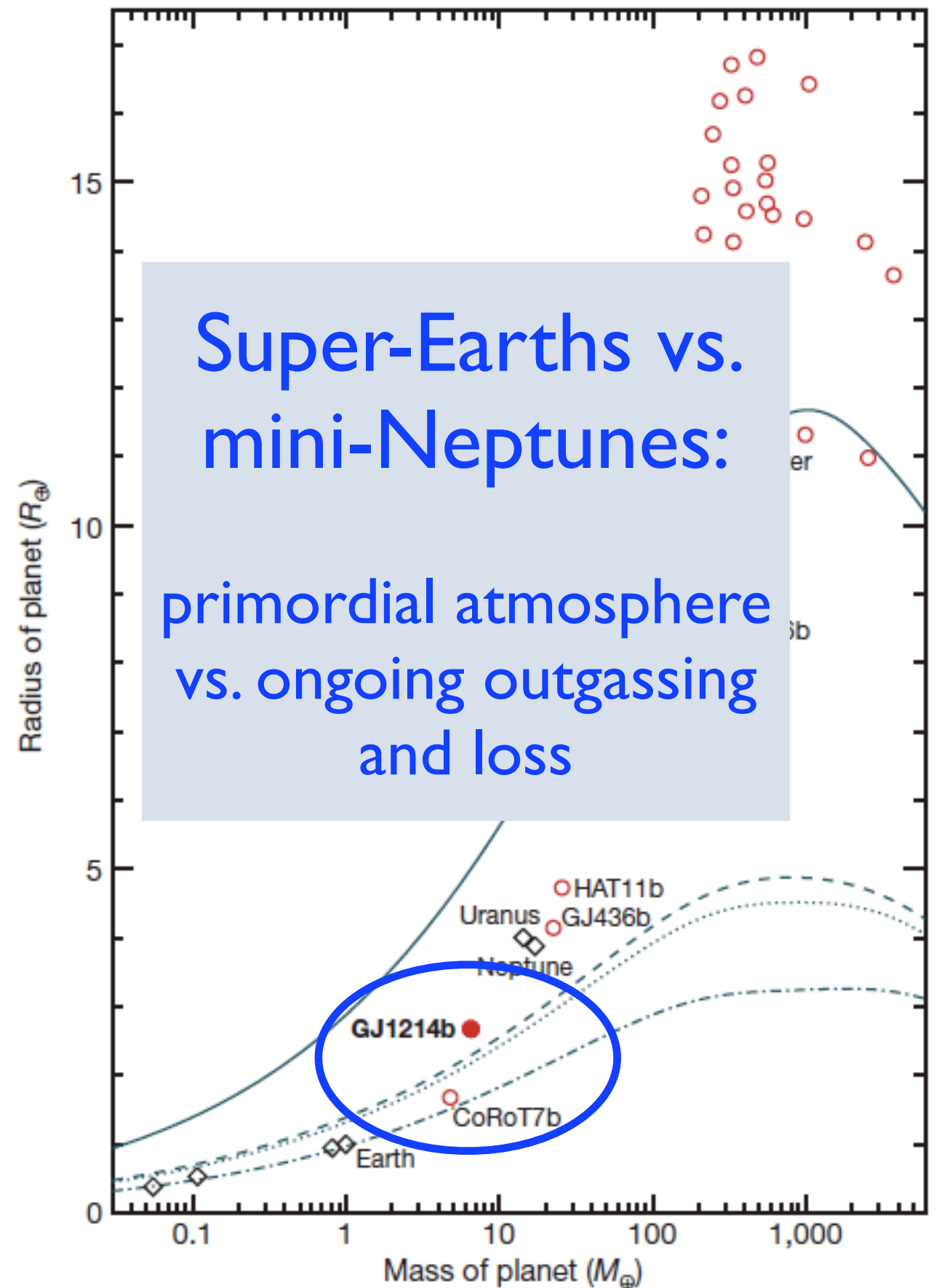
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Summary

- Given UV fluxes typical of hot Jupiters orbiting Sun-like stars, atmospheric escape is \sim hydrodynamic and “energy limited” with $r = R_p$ for observed exoplanets if they have hydrogen-dominated atmospheres, but for smaller radii, beware.
- At lower UV fluxes, beware!
- At higher UV fluxes, beware!
- A practical guide to estimating \dot{M} for hydrogen-dominated atmospheres given FUV, R_p , and M_p will be available soon.